

# Causal Loop Wrap-Up & Stocks-Flow

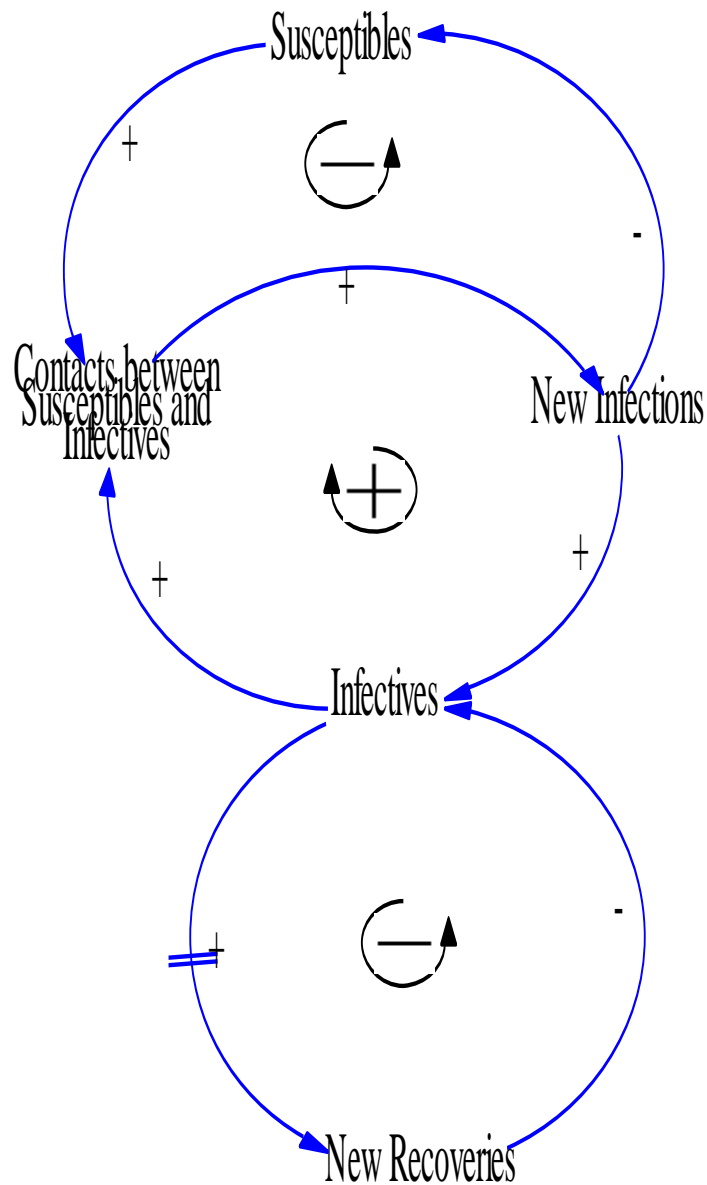
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CMPT 858

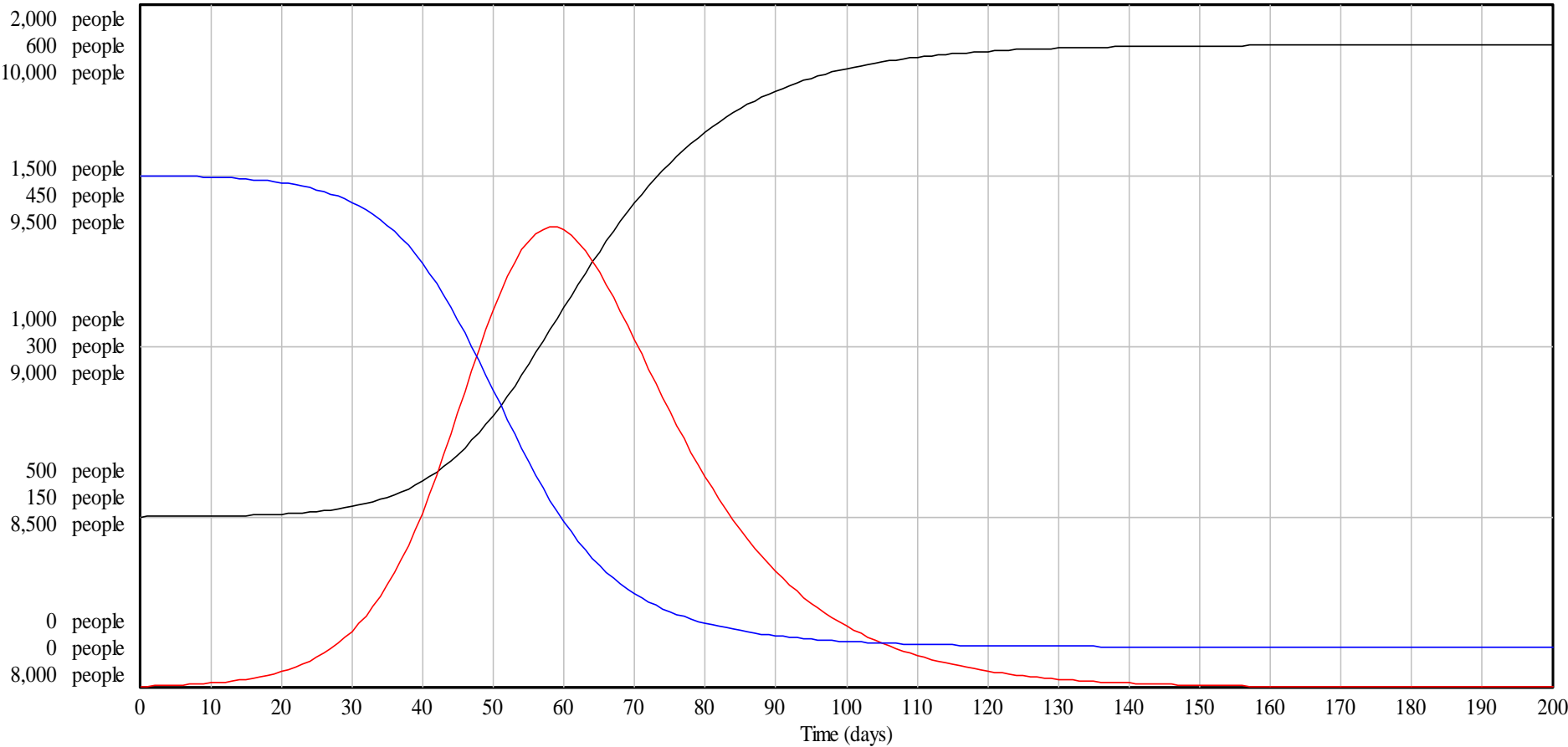
February 4, 2010

# Feedbacks Driving Infectious Disease Dynamics



# Example Dynamics of SIR Model (No Births or Deaths)

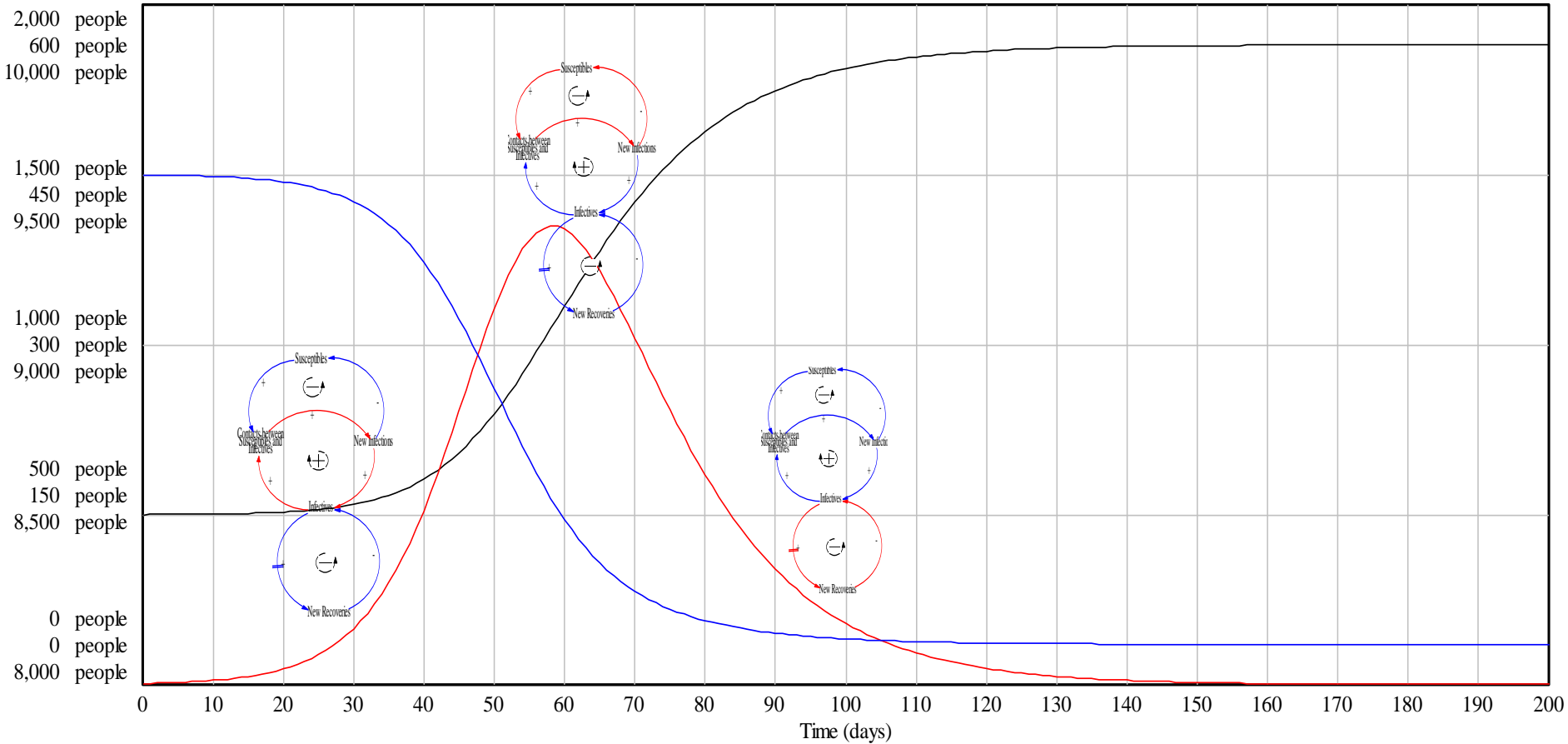
SIR Example



Susceptible Population S : SIR example ————— people  
 Infectious Population I : SIR example ————— people  
 Recovered Population R : SIR example ————— people

# Shifting Feedback Dominance

SIR Example



Susceptible Population S : SIR example ————— people  
 Infectious Population I : SIR example ————— people  
 Recovered Population R : SIR example ————— people

# Issues with Causal Loop Diagrams

- Unclear variables
- Diagrams can become very large
- Confusion regarding polarity
- Non-causal relationship
- Conservation not captured
- Behavior not always same as archetype
- Missing causal factors
- Missing links
- Asymmetry in direction of change

# Unclear Variables

## Variables Lacking Clear Polarity

- Gender
- Ethnicity
- Shape

*Often categorical & non-ordinal*

- Ask whether “more X” is
  - Meaningful
  - Unambiguous

## Implicit Polarity

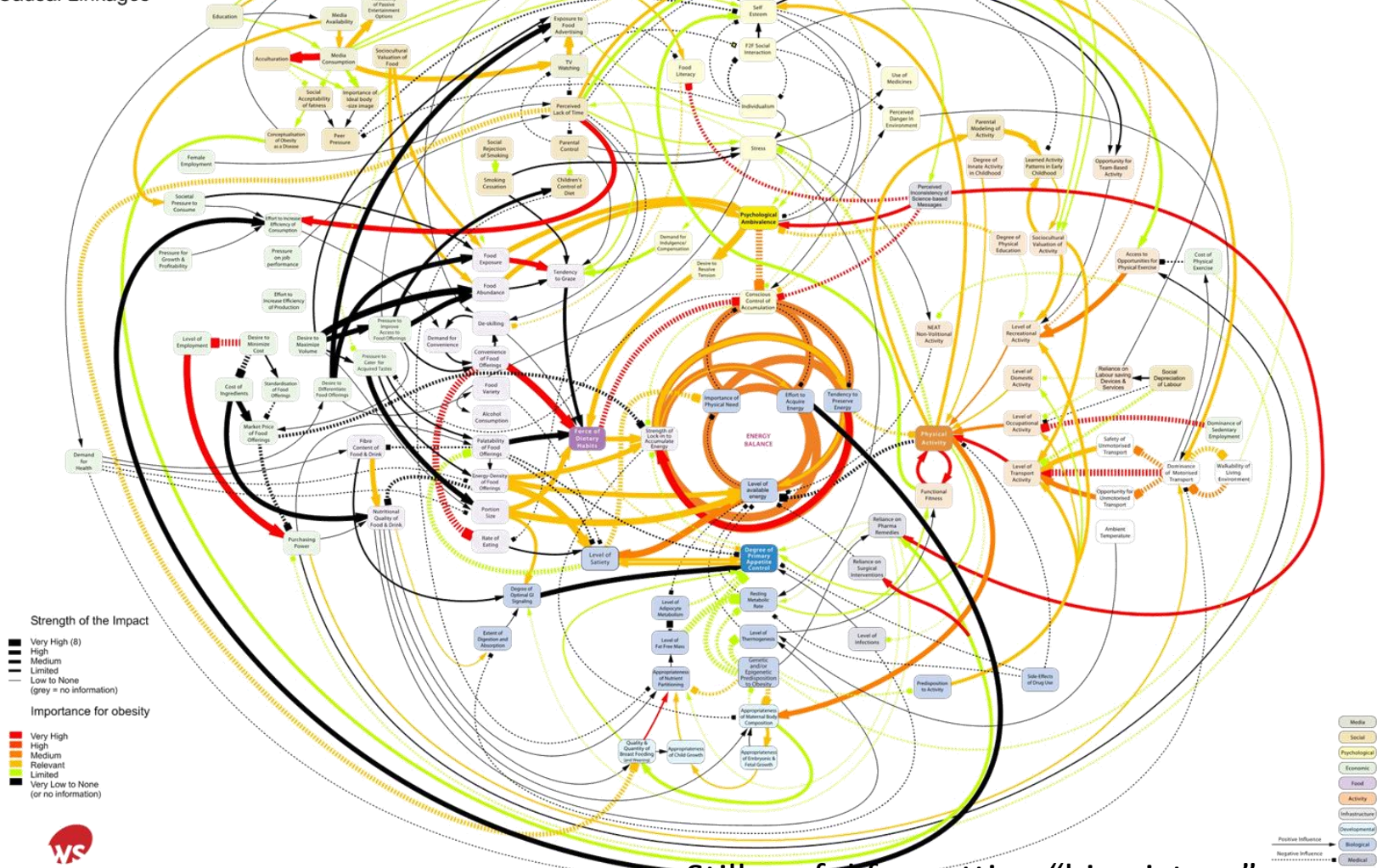
- Population (size)
- Revenue (amount of)
- Sound, Color (more of)
- Socioeconomic status (greater, lesser)

# Very Large Diagrams

Map 27

Obesity System Map  
Version 1.8 - 20 November 2006

Weighted  
Causal Linkages

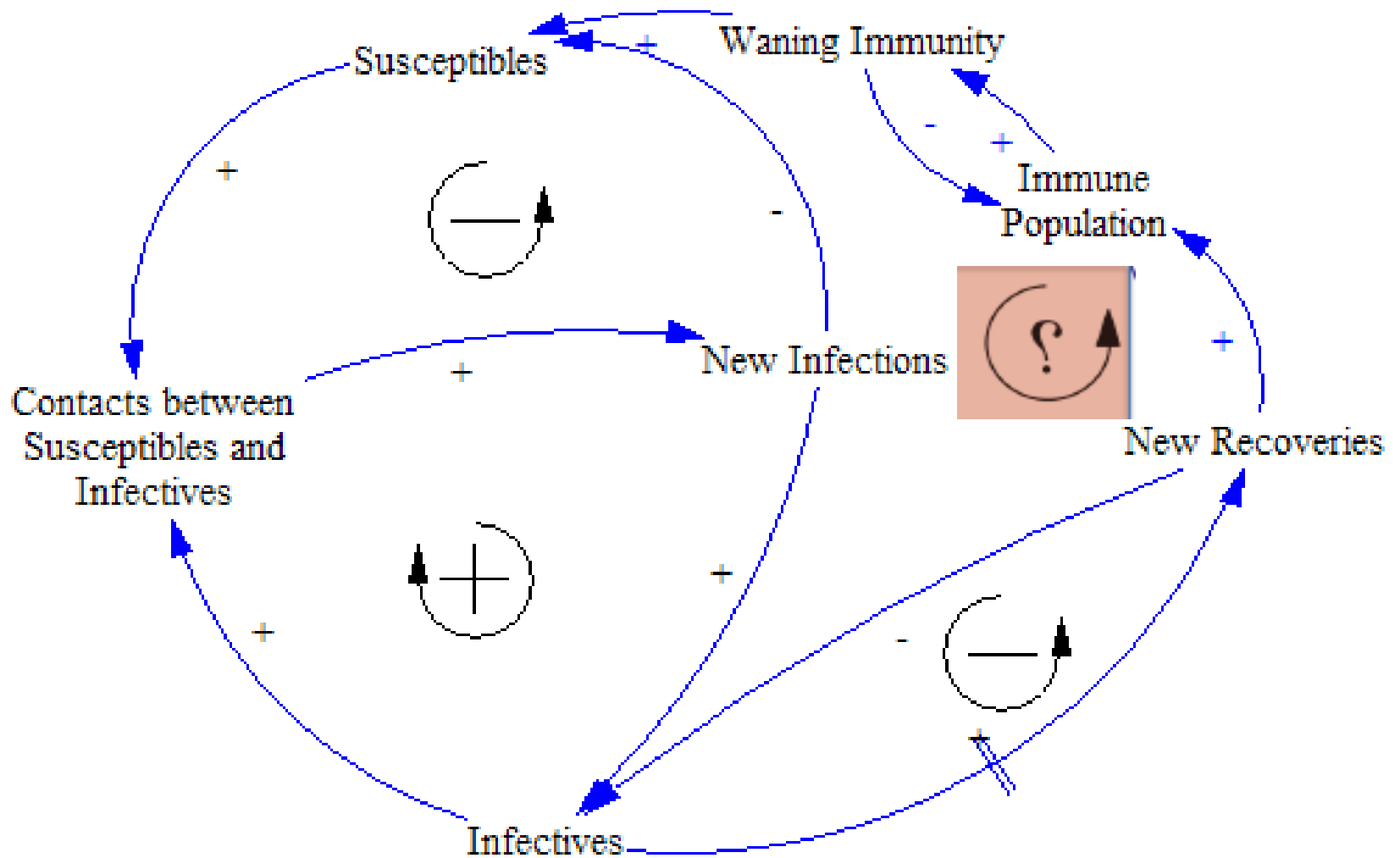


Still useful for getting "big picture"

<http://kim.foresight.gov.uk/Obesity/Obesity.html>

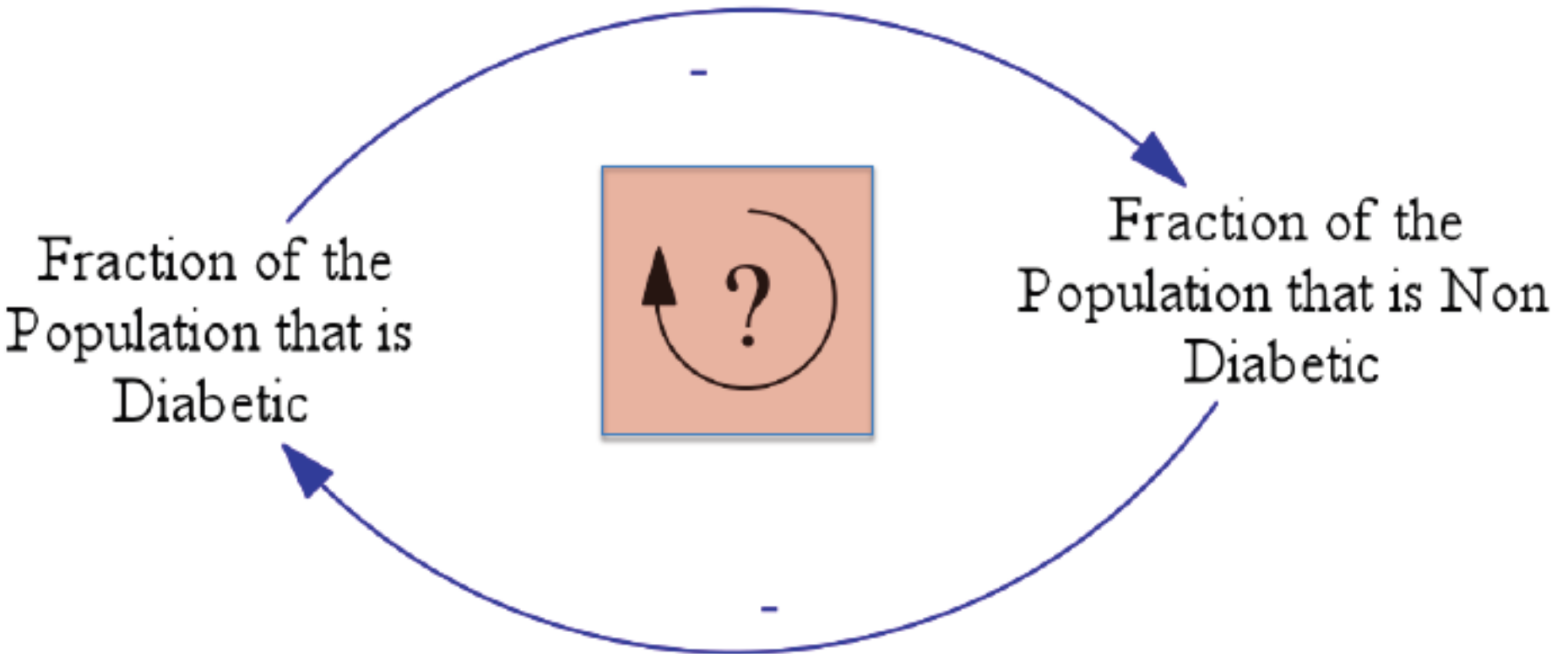
identifying where research "fits in", research gaps

# Artifactual Loop 1

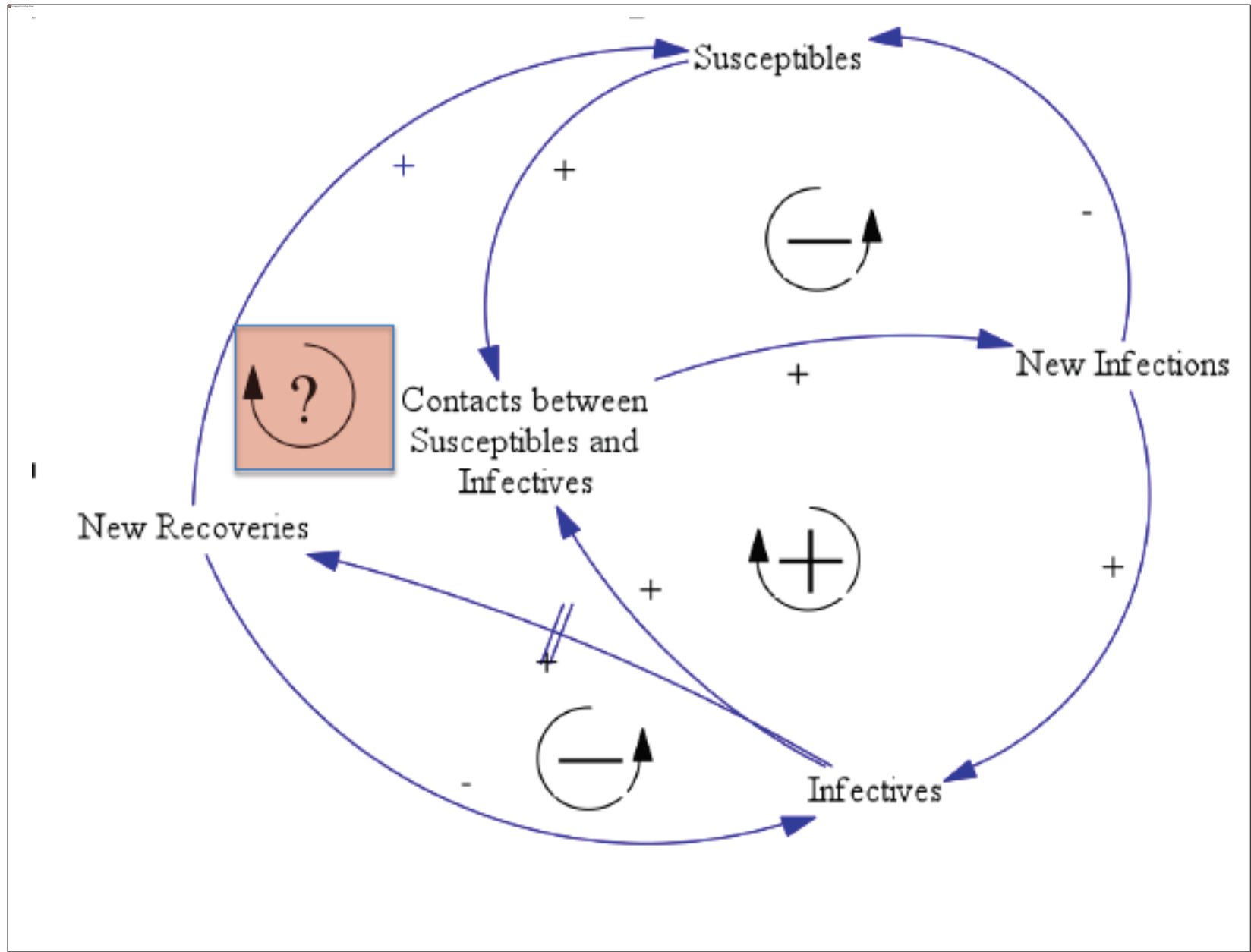




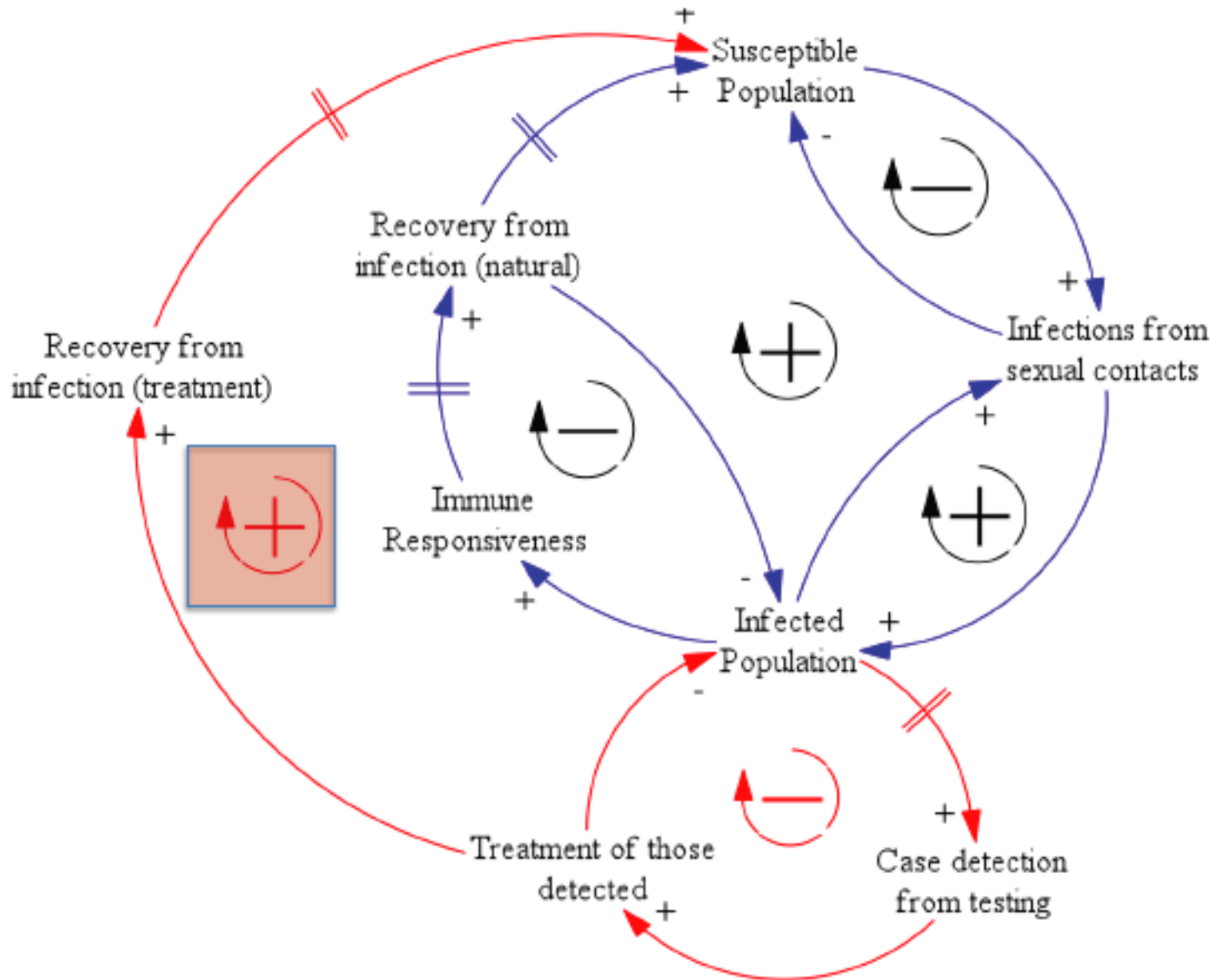
# Artifactual Loop



# Artifactual Loop 2



# Artifactual Loop 3



# Introduction to Stocks & Flows

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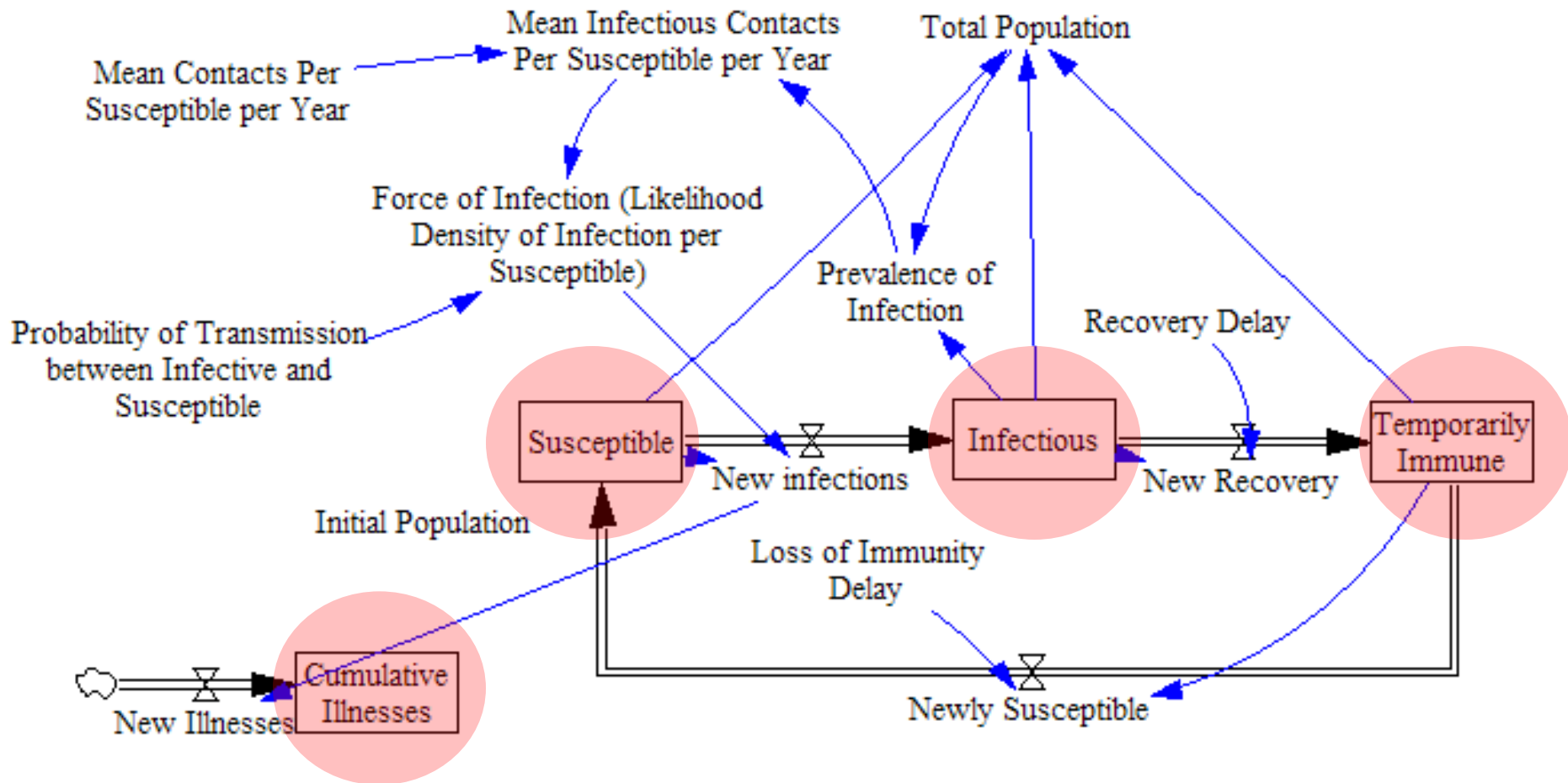
# State of the System: Stocks (“Levels”, “State Variables”, “Compartments”)

- Stocks (Levels) represent accumulations
  - These capture the “state of the system”
  - Mathematically, we will call these “state variables”
- These can be measured at *one instant in time*
- Stocks start with some initial value & are thereafter changed only by *flows* into & out of them
  - There are no inputs that immediately change stocks
- Stocks are the source of delay in a system
- In a stock & flow diagram, shown as ***rectangles***

# Examples of Stocks

- Water in a tub or reservoir
- People of different types
  - {Susceptible, infective, immune} people
  - Pregnant women
  - Women between the age of  $x$  and  $y$
  - High-risk individuals
- Healthcare workers
- Medicine in stocks
- Money in bank account
- CO<sub>2</sub> in atmosphere
- Blood sugar
- Stored Energy
- Degree of belief in  $X$
- Stockpiled vaccines
- Goods in a warehouse
- Beds in an emergency room
- Owned vehicles

# Example Model: Stocks



# The Critical Role of Stocks in Dynamics

- Stocks determine current state of system
  - Stocks often provide the basis for making choices
- Stocks central to most disequilibria phenomena (buildup, decay)
- Lead to inertia
- Give rise to delays



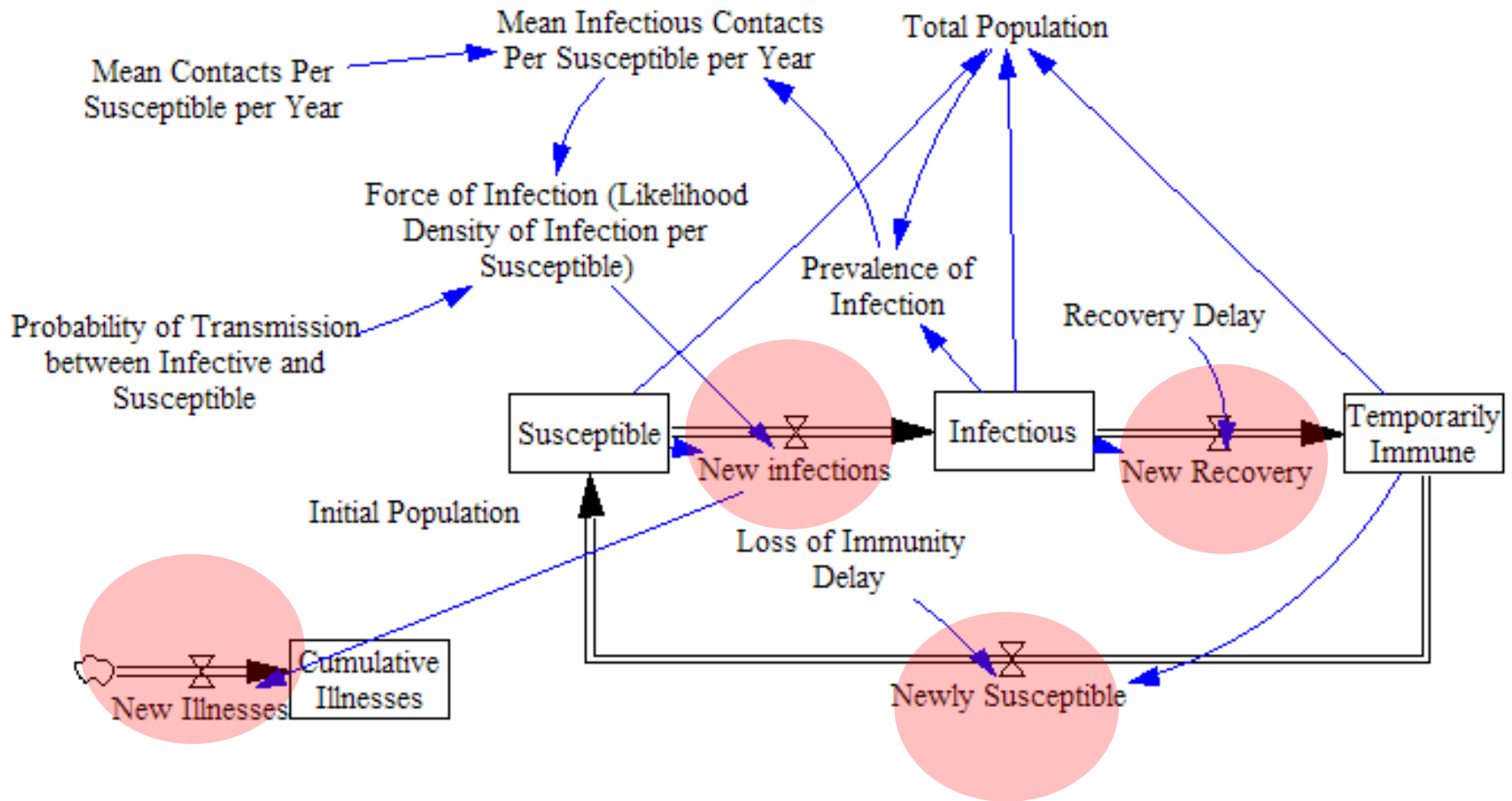
# State Changes: Flows (“Fluxes”, “Rates”, “Derivatives”)

- All changes to stocks occur via *flows*
- Always expressed per some unit time: If these flow into/out of a stock that keeps track of things of type  $X$  (e.g. persons), the rates are measured in  $X/(\text{Time Unit})$  (e.g. persons/year, \$/month, gallons/second)
- Typically measure over certain period of time (by considering accumulated quantity over a period of time)
  - e.g. Incidence Rates is calculated by accumulating people over a year, revenue is \$/Time, water flow is litres/minute
  - Can be estimated for any point in time

# Examples of Flows

- Inflow or outflow of a bathtub (litres/minute)
- Rate of incident cases (e.g. people/month)
- Rate of recovery
- Rate of mortality (e.g. people/year)
- Rate of births (e.g. babies/year)
- Rate of treatment (people/day)
- Rate of caloric consumption (kcal/day)
- Rate of pregnancies (pregnancies/month)
- Reactivation Rate (# of TB cases reactivating per unit time)
- Revenue (\$/month)
- Spending rate (\$/month)
- Power (Watts)
- Rate of energy expenditure
- Vehicle sales
- Vaccine sales
- Shipping rate of goods

# Example Model: Flows



# Flows 2

- We can ask conceptually *about* the rate *at* any given point in time – and may change over time
  - Measuring it would have to be over some period
- When speaking about “rates” for flows, we always mean a *rate of change over time* (something measured as *X/Unit Time*)
  - Not all things called “rates” are flows
    - Exchange rate
    - Prevalence rate
    - Rate of return

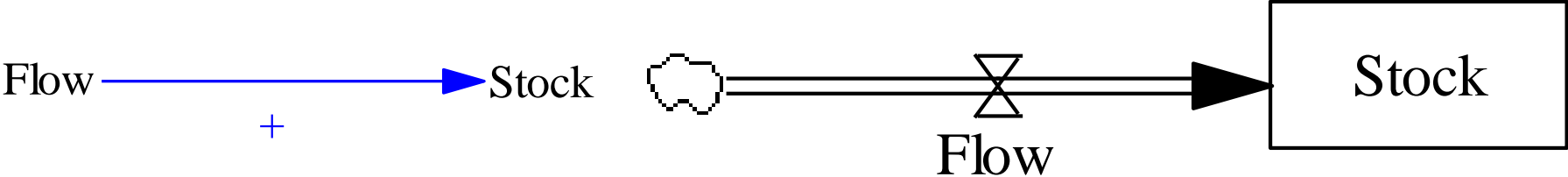
# Distinguishing Stocks & Flows: Heuristics

- To determine if a quantity is a stock or flow:
  - “Snapshot” test: If you were only to consider a moment in time (a “snapshot” of the system), could the quantity be clearly quantified by the information available at that moment?
    - If yes, stock (cannot quantify a value of a flow using only the information for an instant – must measure over time)
  - “Time unit change” test: If we were to change the unit by which we measure time, would the numeric value of the quantity change?
    - If yes, quite likely to be a *flow* (exception: beliefs about flows)
  - “Accumulation” test: Is this quantity an accumulation of the time-varying values of other quantities?
    - If yes, stock

# Exercise: Stocks or Flows?

- Account balance
- Income
- Incidence
- Prevalence
- Temperature
- Births
- Profits
- Interest
- Principal
- Shipments
- Car accidents
- Patients on dialysis
- Deaths
- Heart attacks
- Arrests
- Police
- Patients in hospital
- Hospital admissions
- Position
- Speed

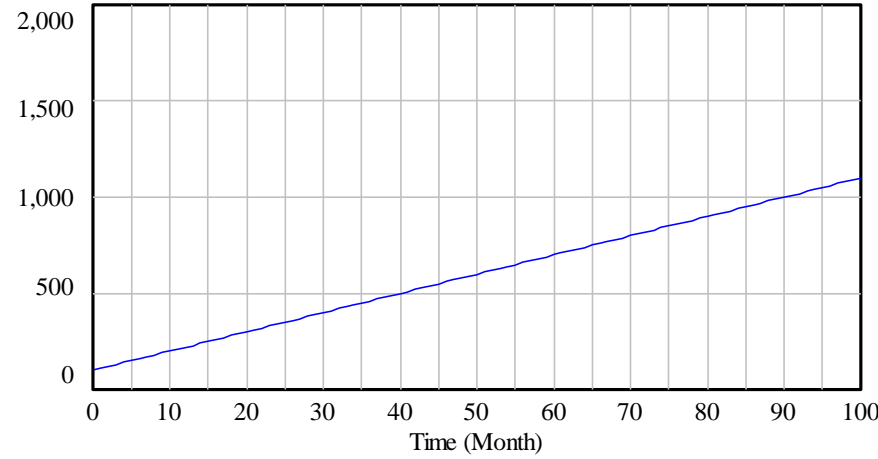
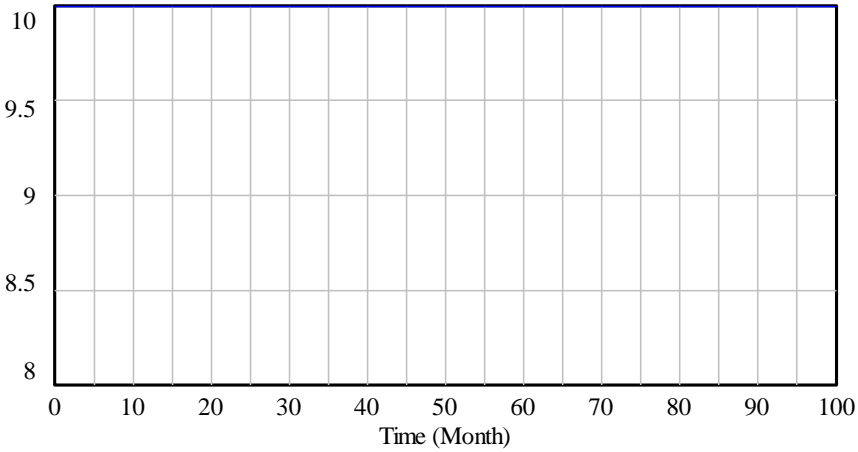
# Key Component: Stock & Flow



# Net Flow Impact on Stock

Flow

Stock



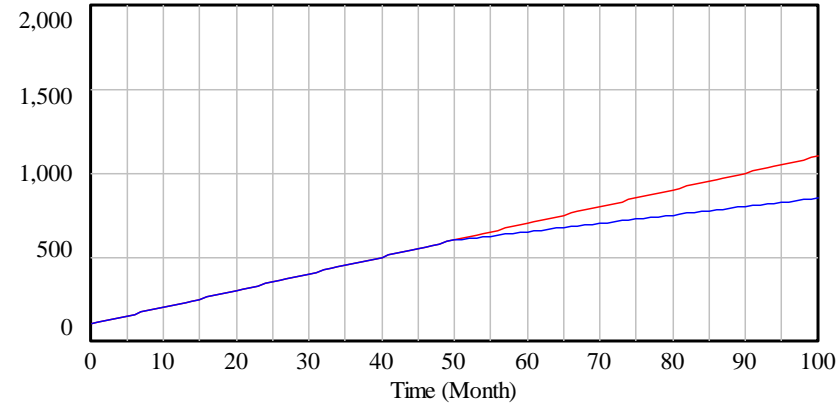
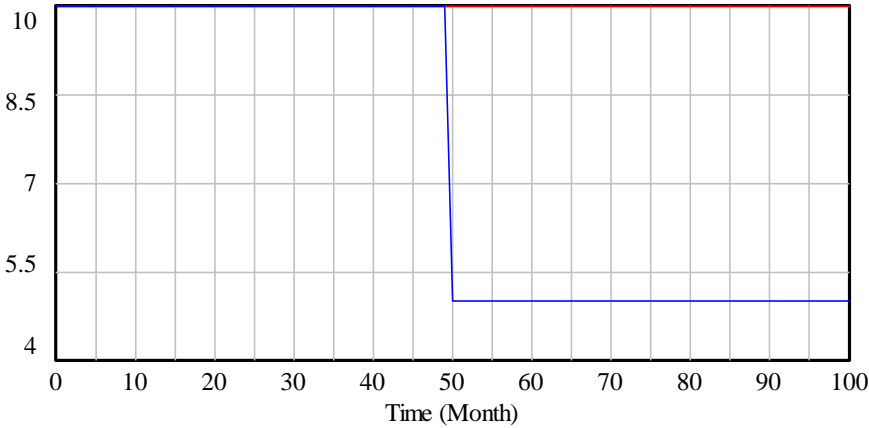
Flow : Current 

Stock : Current 

## Impact of Lowering Flow (Rate) to 5/Month?

Flow

Stock



Flow : Stock and Flow Alternative 

Flow : Current 

Stock : Stock and Flow Alternative 

Stock : Current 



# Loops & Stocks

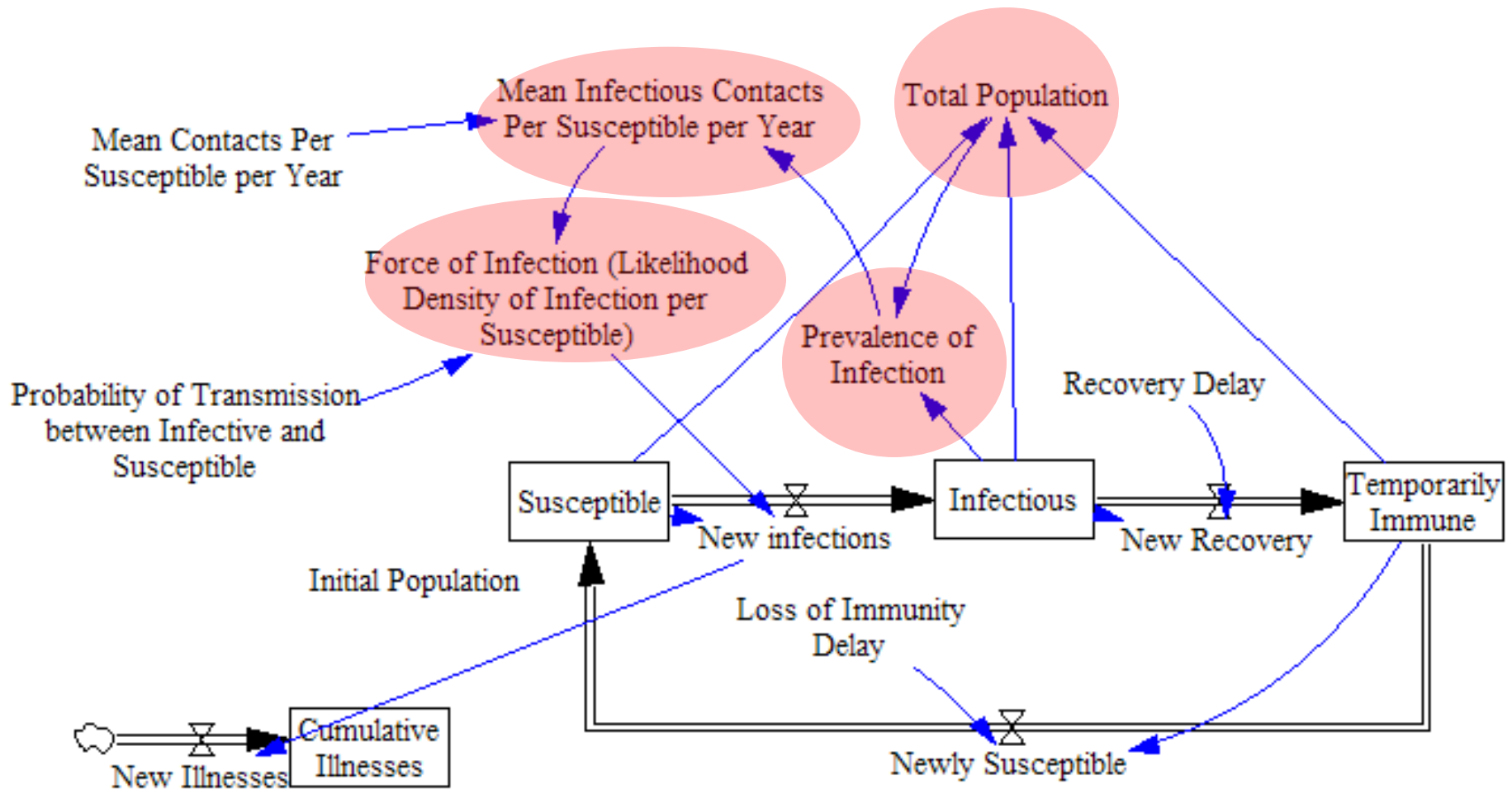
- Causation does not effect big change instantaneously
  - Loops are not instantaneous
- Stocks only change by changes to the flows into & out of them
  - There are no inputs that immediately change stocks
- All causal loops must involve at least one stock
  - The state of the world must change as part of the process
  - Absent a stock, loop would be instantaneous

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Redacted from Public PDF for Copyright  
Reasons

# Auxiliary Variables

- Auxiliary variables are convenience names we give to concepts that can be defined in terms of expressions involving stocks/flows at current time
  - Adding or eliminating an auxiliary variable does not change the mathematical structure of the system
- Critical for model transparency
  - Can be reused at many places
  - References to auxiliary variables prevents need for modeler to think about all of details of definition
- Enhanced modifiability: Single place to define
- Convenient for reporting (graphing, tables) & analyzing model dynamics

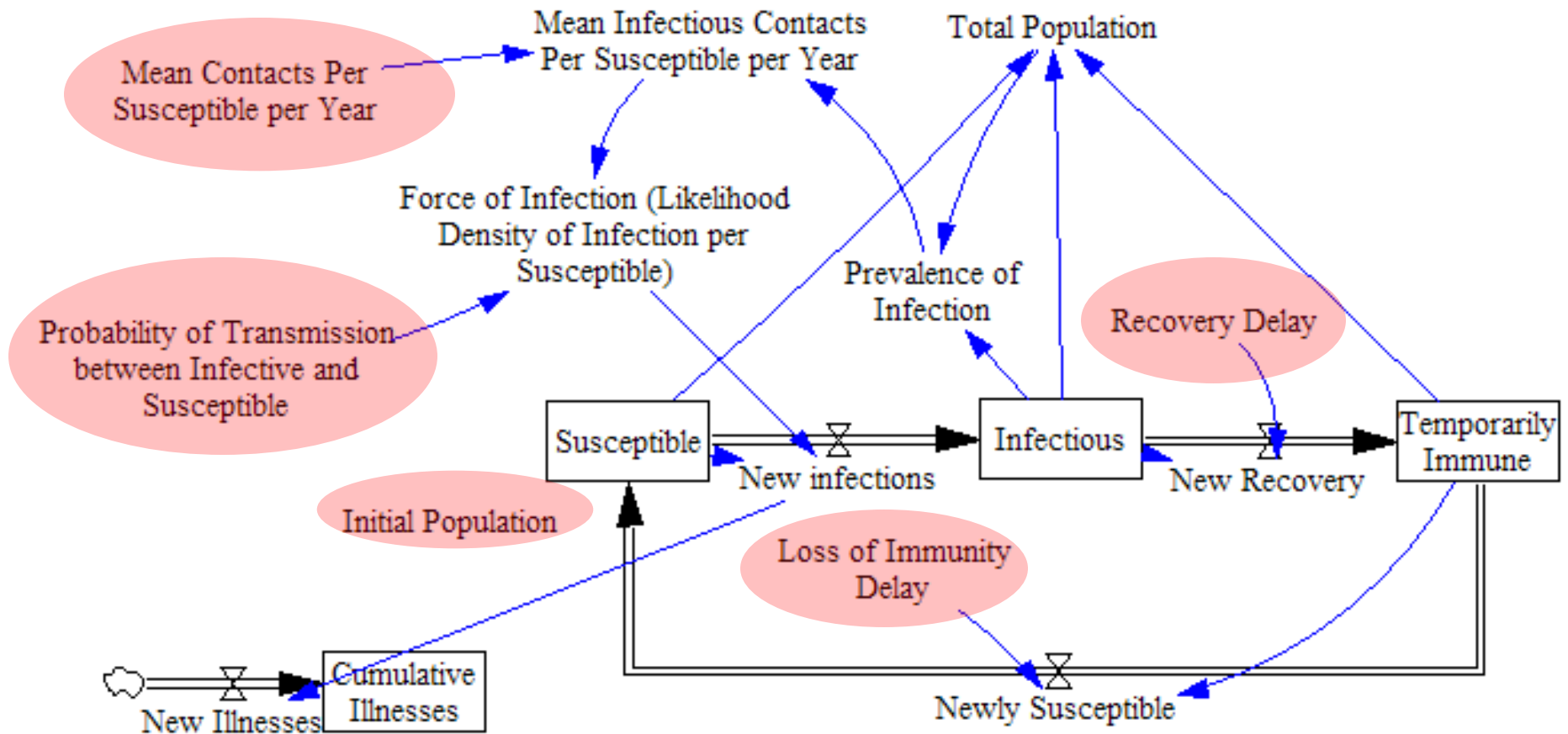
# Example Model: Auxiliary Variables



# Constants & Time Series Parameters

- For similar reasons to auxiliary variables, we give names to
  - Model constants
  - Time series

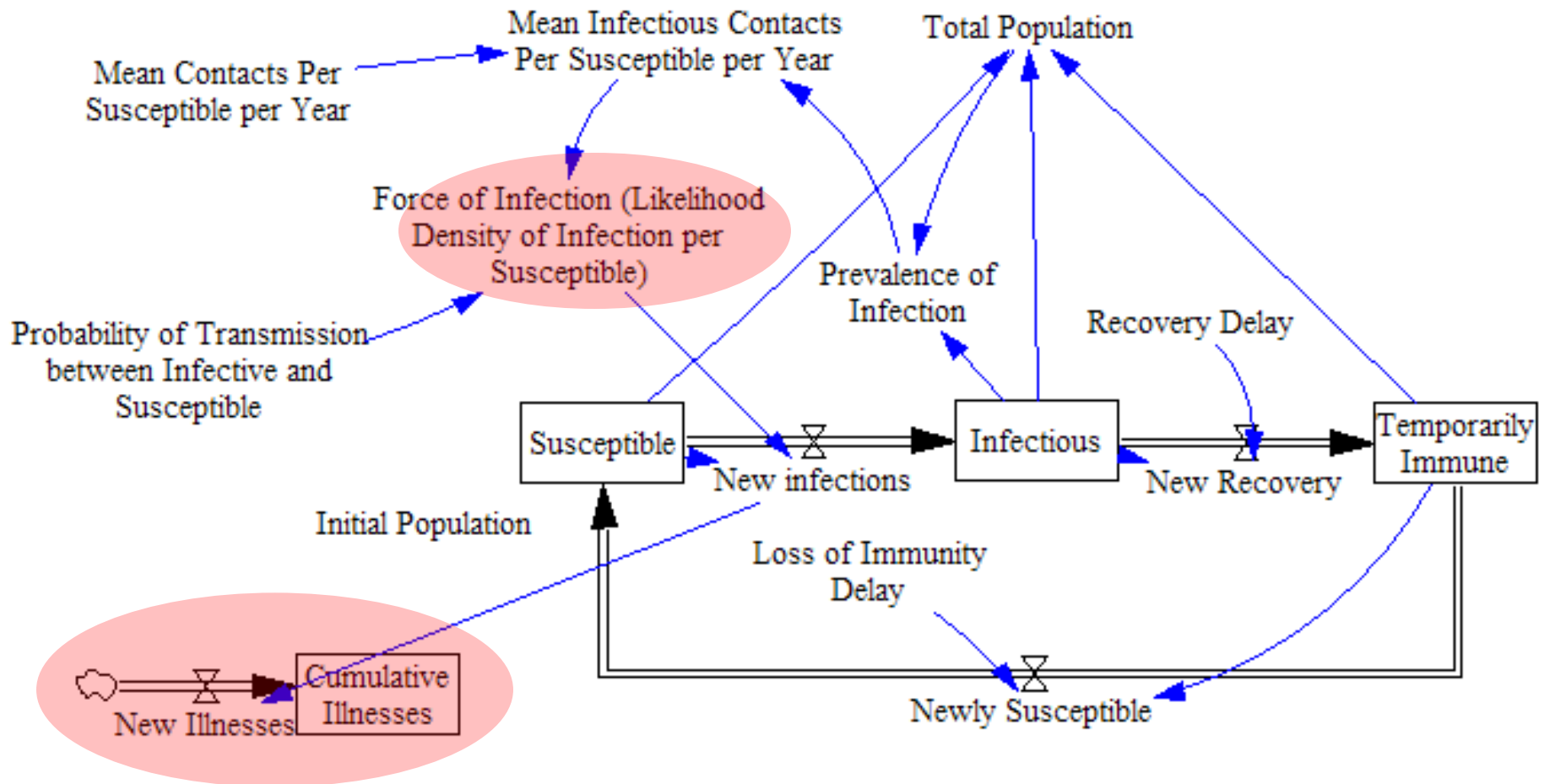
# Example Model: Parameters



# Stocks & Flows Compared with Markov Models

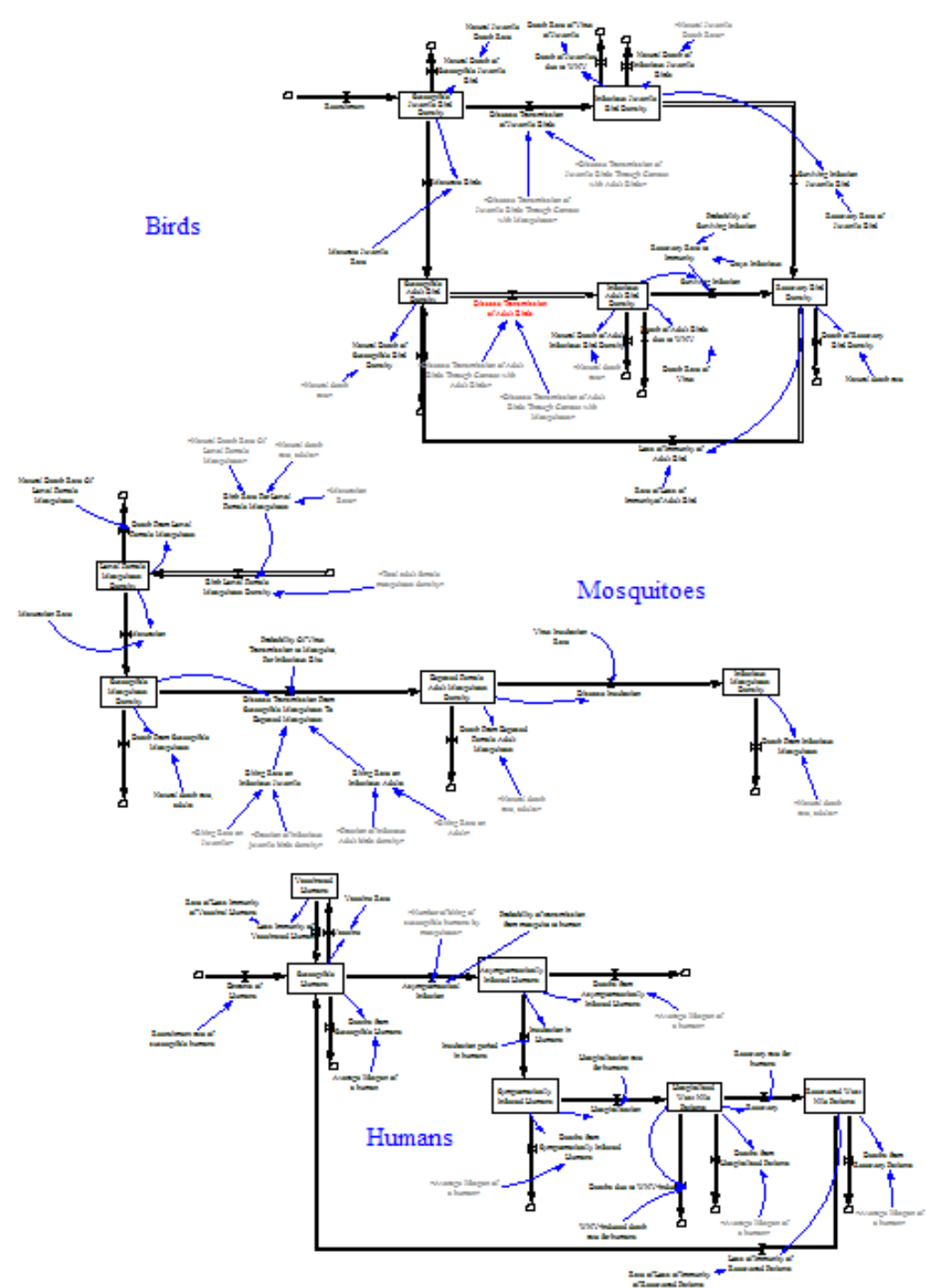
- Open population
  - Births
  - Deaths
- Non-constant likelihood (density) of transitions
  - Likelihood of leaving a stock per unit time can depend on other stocks
    - Force of Infection (likelihood of susceptible becoming infected) can depend on prevalence of illness
    - Likelihood of initiating smoking could depend on accumulated current or former smokers
- Multiple types of stocks
  - e.g. costs, QALYs, hosts & reservoir species, etc.
- Continuous time

# Distinctive Stock & Flow Features





# Multi-Species Model (West Nile Virus)



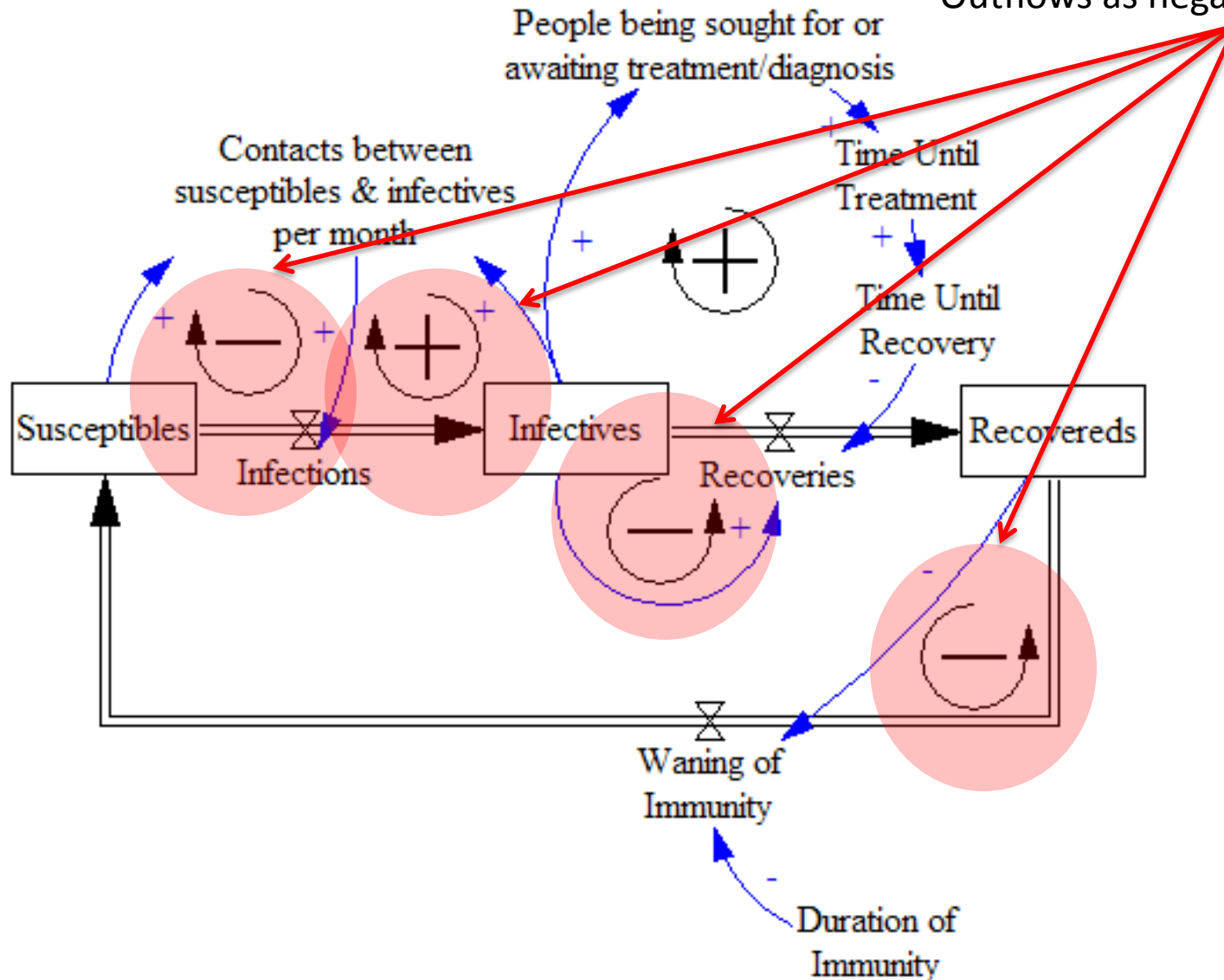
# Refinement of Causal Loop Diagrams: System Structure Diagrams

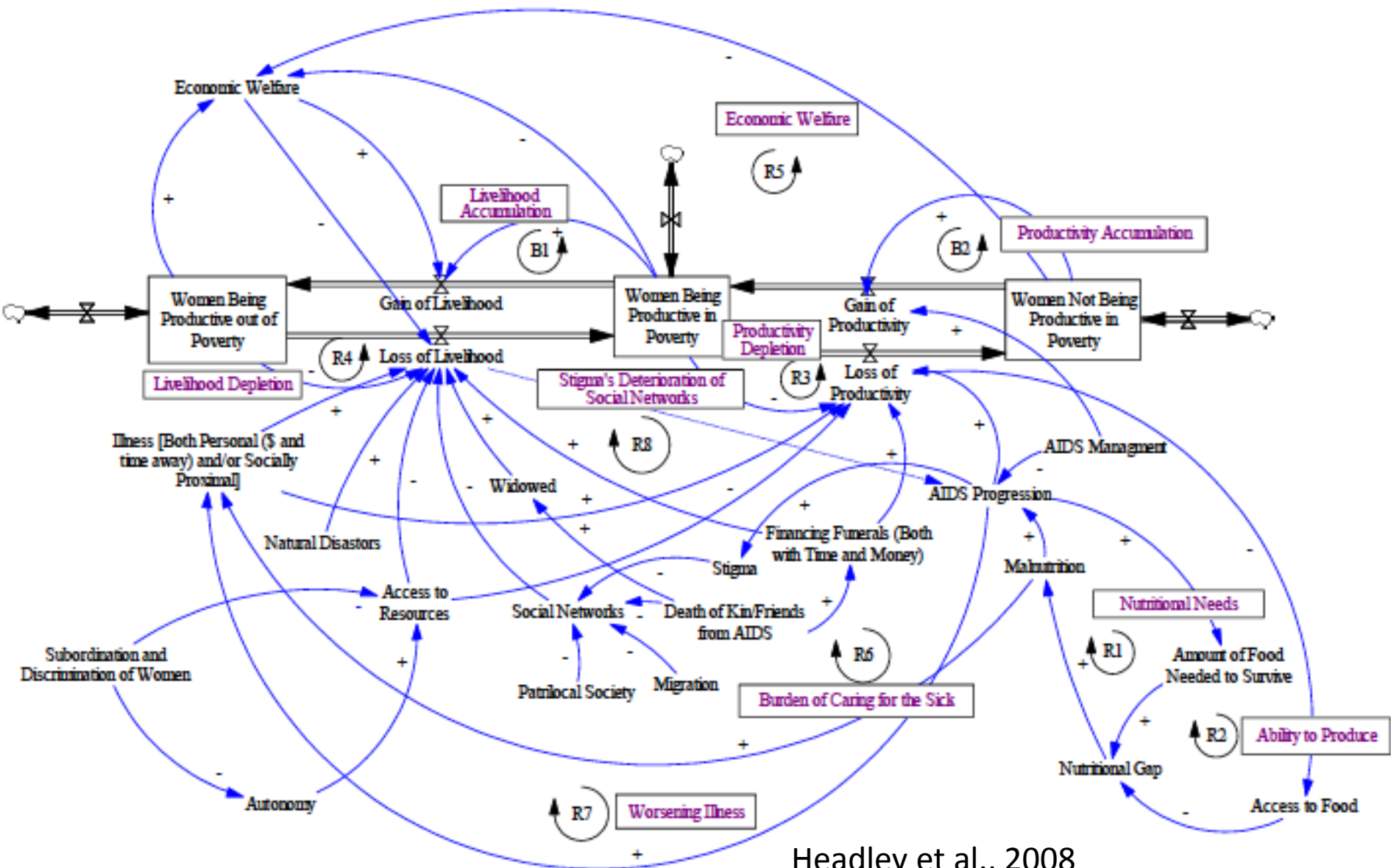
- Still essentially a qualitative model, but less ambiguous
  - By clearly distinguish stocks & flows, this helps reduce the artifactual loops discussed with CLDs
- Combine causal loops diagram elements with stock & flow structure
- If complete, all loops will go “through a stock”
  - Loop goes into the flow of a stock (as one variable in the diagram)
  - Loop comes out of stock (as next variable in diagram)

# Example System Structure Diagram

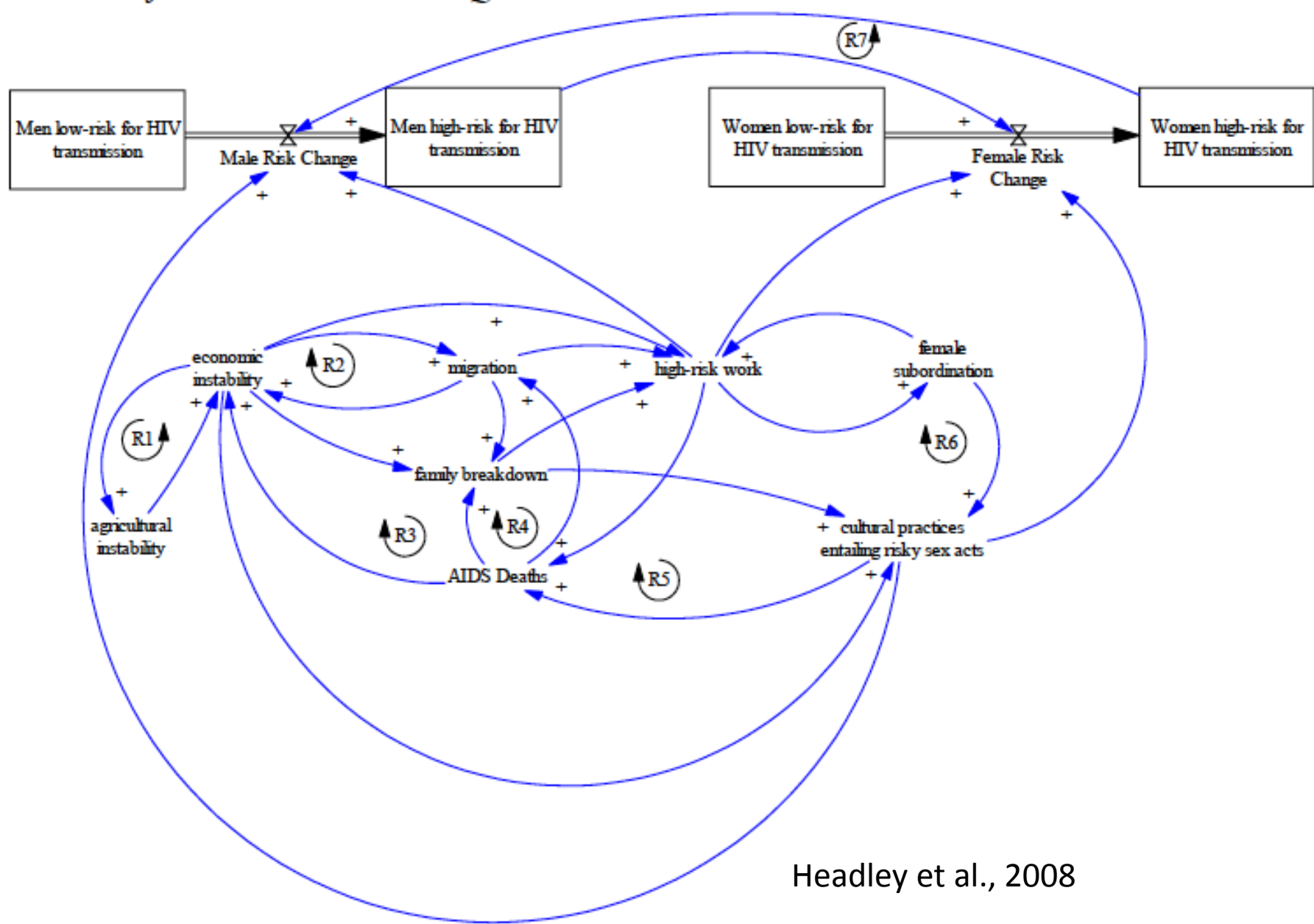
Note treatment of flows as links from flow to stock

- Inflows as positive links
- Outflows as negative links

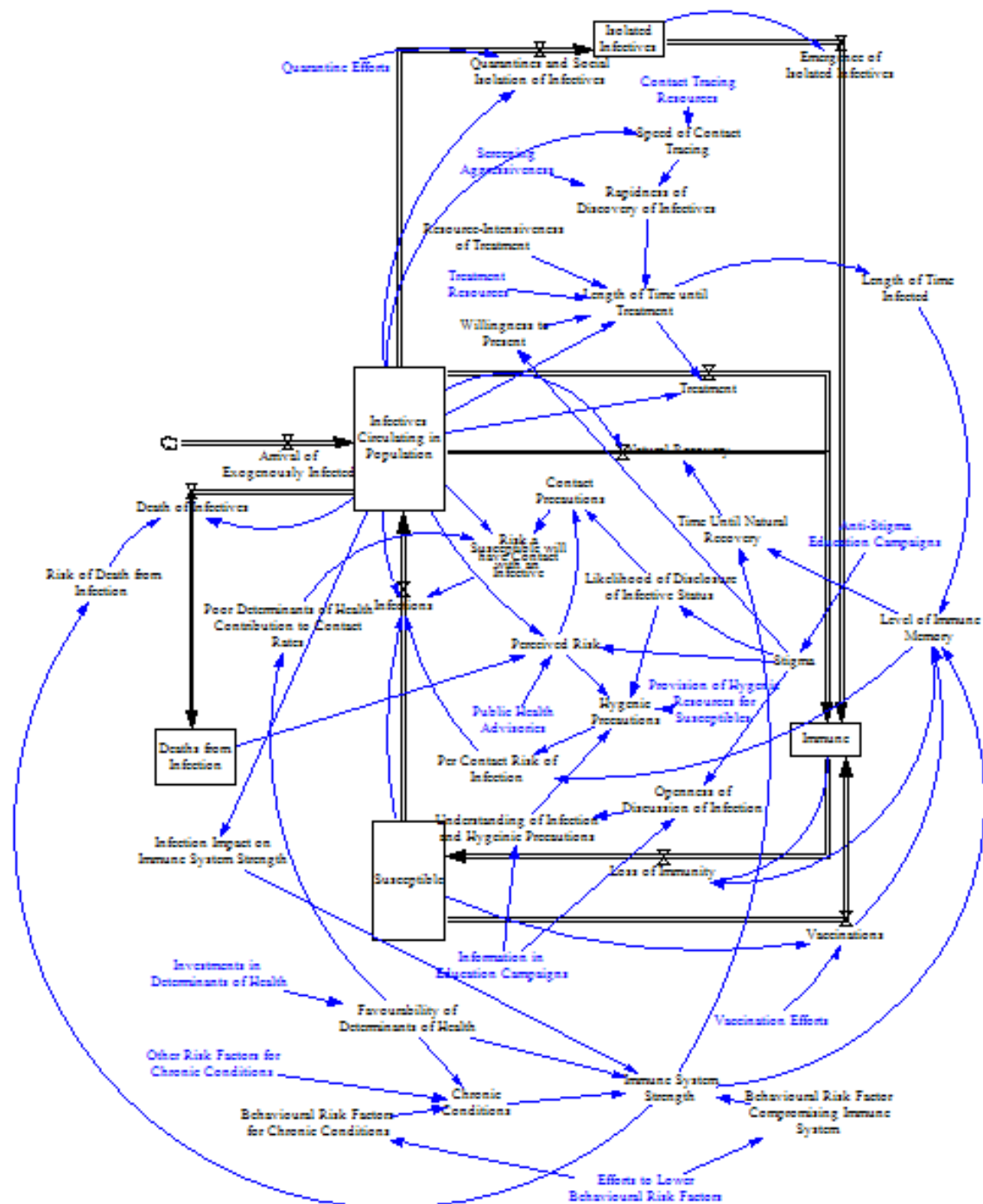




Headley et al., 2008



Headley et al., 2008



# Stocks & Flows: Diabetes

- Assume diabetes is not curable
- Stocks:
  - People without diabetes (at different stages of risk?)
  - People with diabetes
- Flows
  - Incident cases (both diagnosed & undiagnosed!)
  - Deaths from both stocks

# Stocks & Flows: Tuberculosis

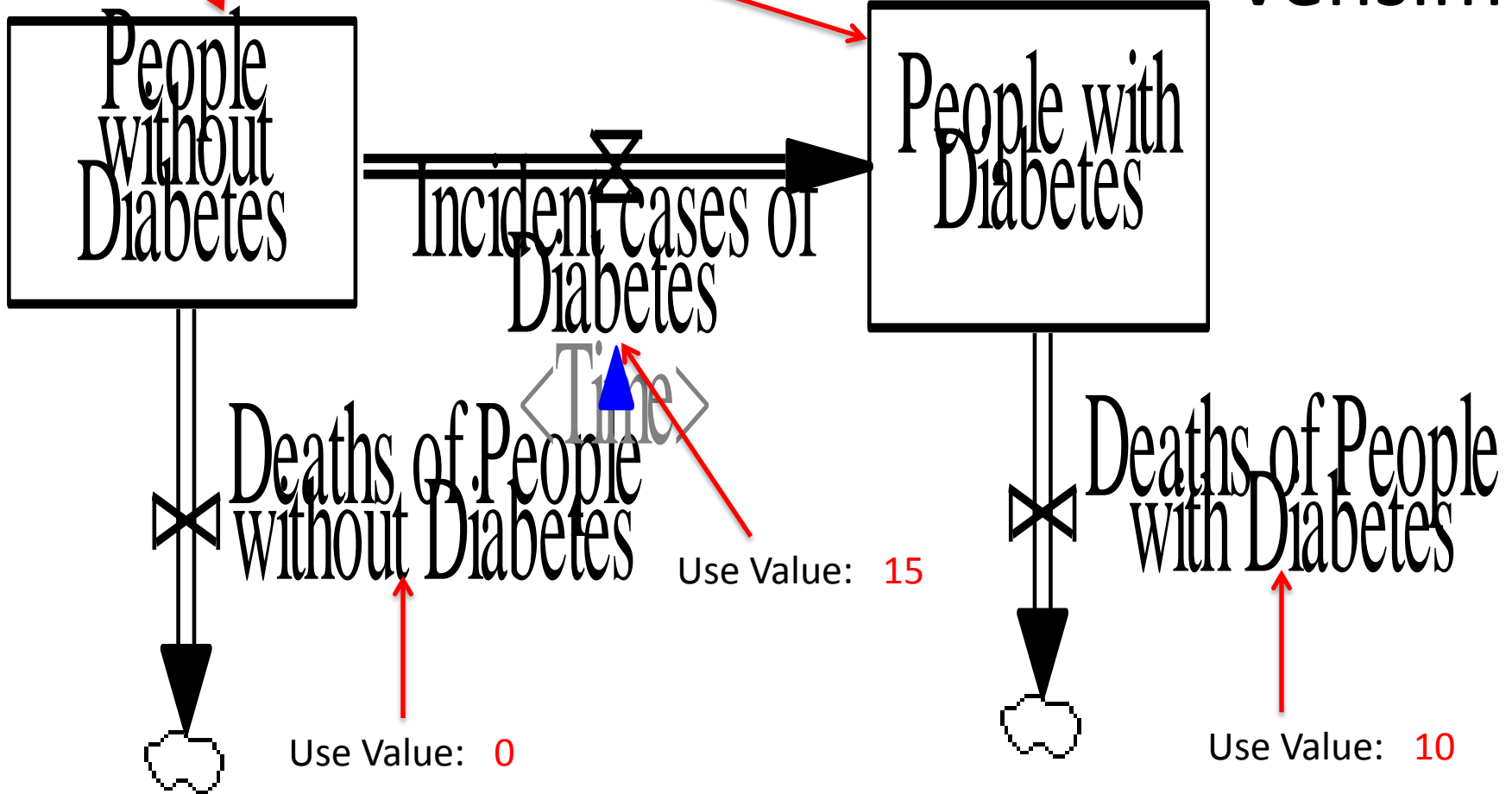
- Assume that TB infection cannot be totally eliminated
- Stocks
  - Susceptible people
  - Immunized people
  - People with latent TB infection
  - People with active TB infection
- Flows
  - People becoming latently infected
  - People being vaccinated
  - People with infection going to Active TB (“primary progression”)
  - People with infection going on to latent TB
  - People with secondary infection going on to active TB
  - Deaths from each stock



# Diabetes Model Stocks & Flows

Use Initial Value: 1000

(For a Challenge, Try Creating this in Vensim!)

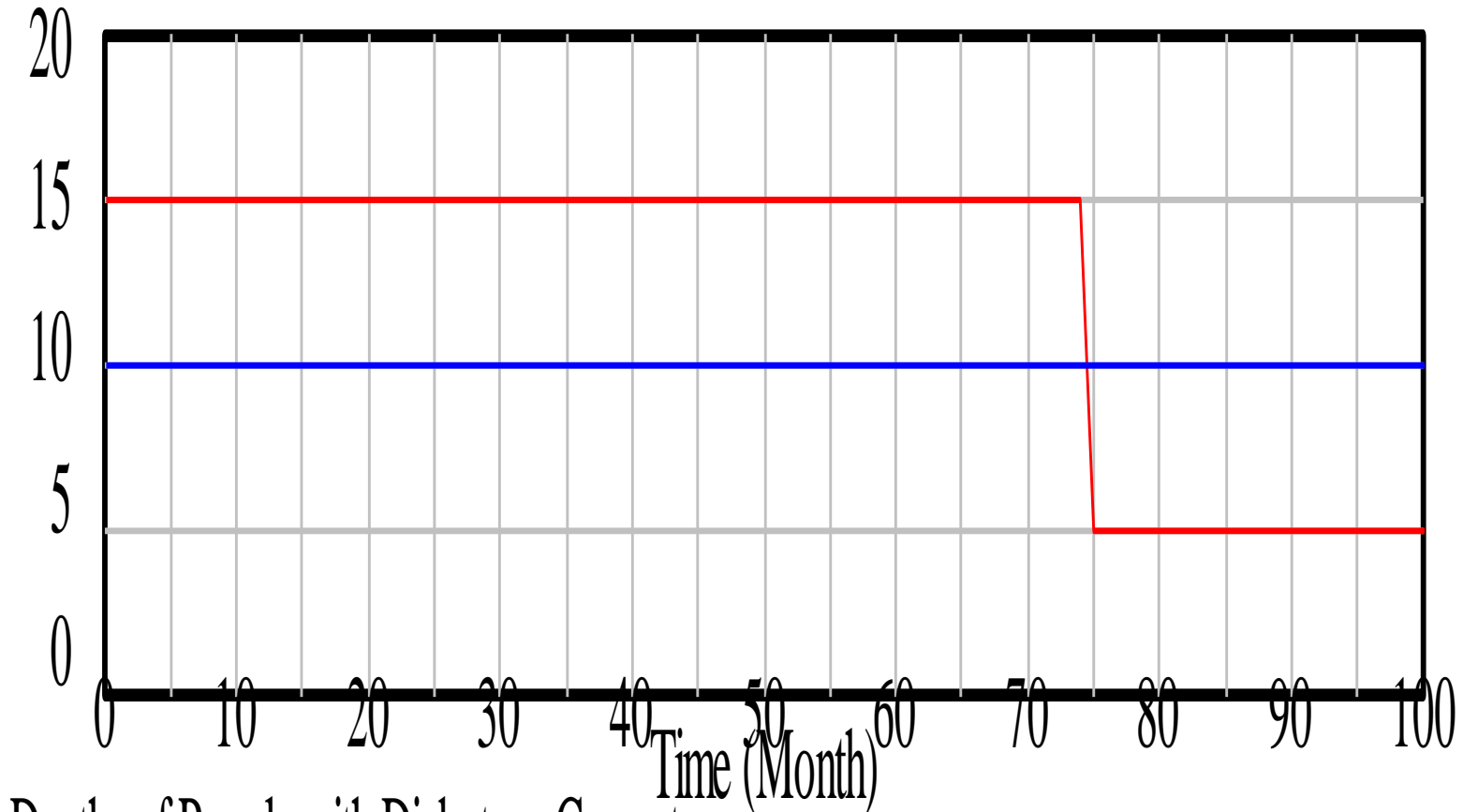


# Interactive Steps

- View flows and stocks – does this make sense?
- Hitch up constant “auxiliary” variables to flows
- How does changing constant variables change the stock?

# Constant Flows

Diabetes Flows

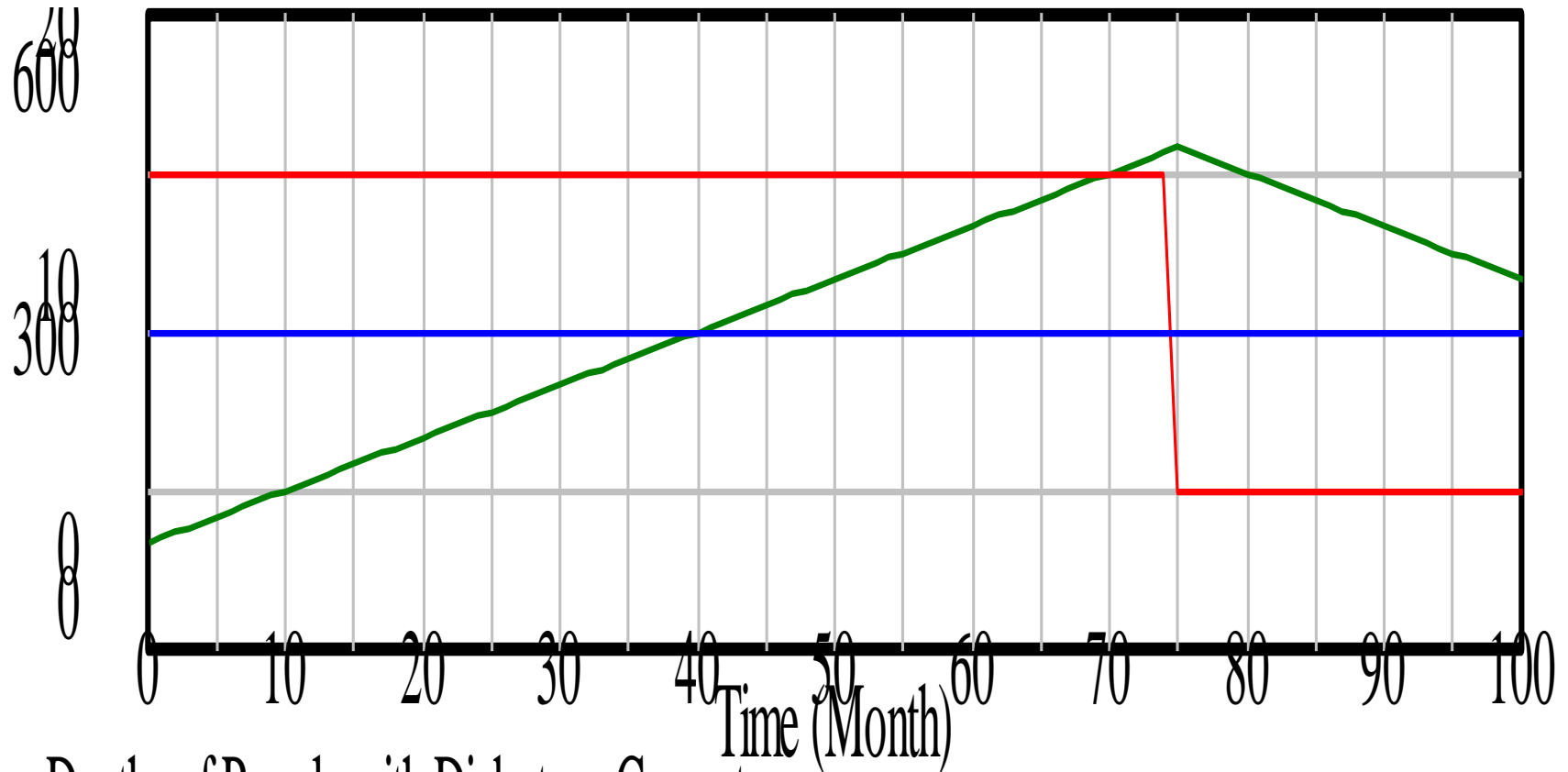


Deaths of People with Diabetes : Current

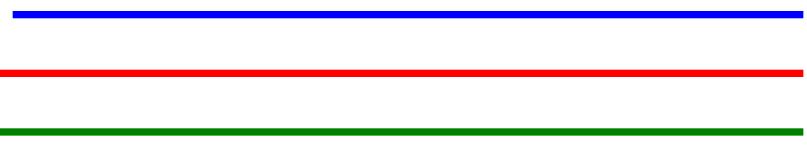
Incident cases of Diabetes : Current

**What happens to the stock?**

# Resulting Stock (Green)

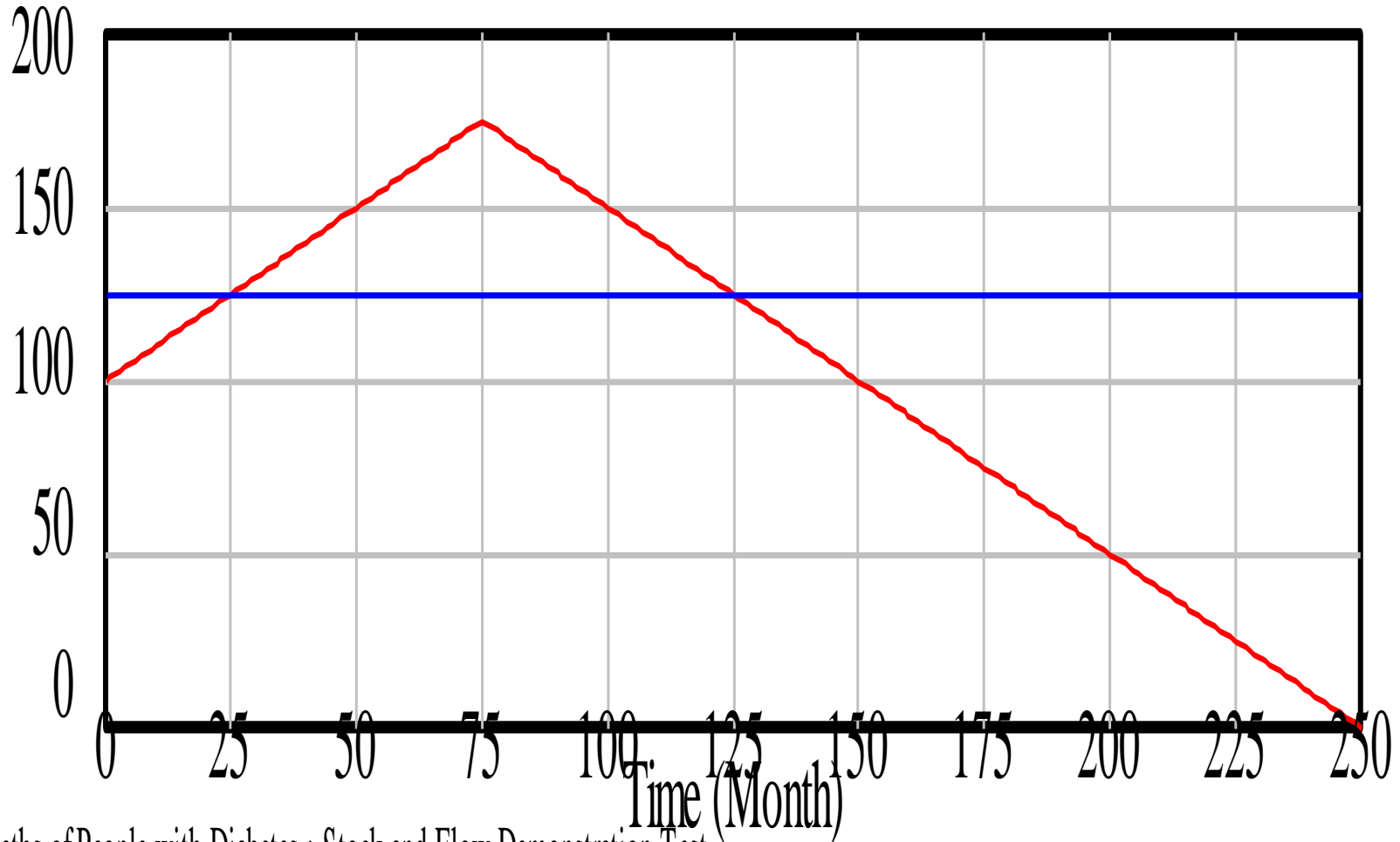


Deaths of People with Diabetes : Current  
Incident cases of Diabetes : Current  
People with Diabetes : Current



# Suppose we have these Flows (Rates)

## Diabetes Flows

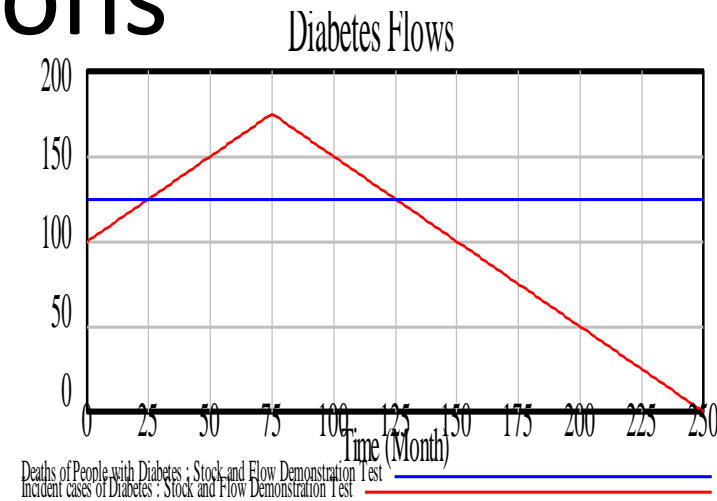


Deaths of People with Diabetes : Stock and Flow Demonstration Test  
Incident cases of Diabetes : Stock and Flow Demonstration Test

**What happens to the stock?**

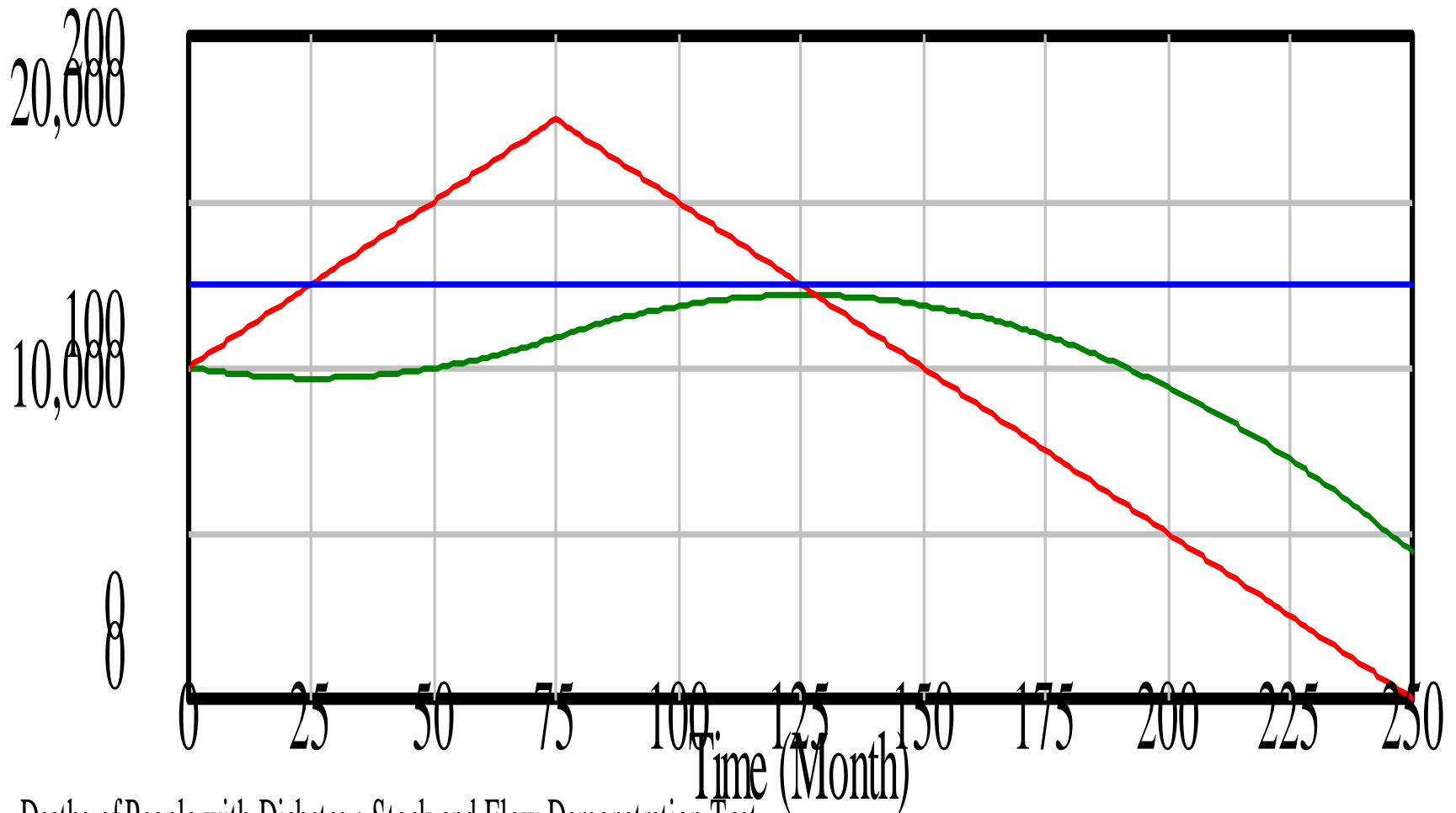
# Some Questions

- When is the stock of people with diabetes at its lowest value?
- When is the stock of people with diabetes at its greatest value?
- Is the value of the stock of people with diabetes larger at the beginning or end?
- When is the stock of people with diabetes not changing?

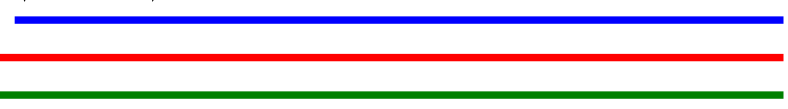


# Stock (Green)

## Diabetes Stock & Flows



Deaths of People with Diabetes : Stock and Flow Demonstration Test  
Incident cases of Diabetes : Stock and Flow Demonstration Test  
People with Diabetes : Stock and Flow Demonstration Test



# Flows and Feedbacks

- Stocks are always changed by flows
- In your experiments, we've used constant values for flows
- In general, the formulas for the flows will depend on things that are changing (state)
  - Ultimately, these things must depend on the things that collectively specify the state – the stocks!

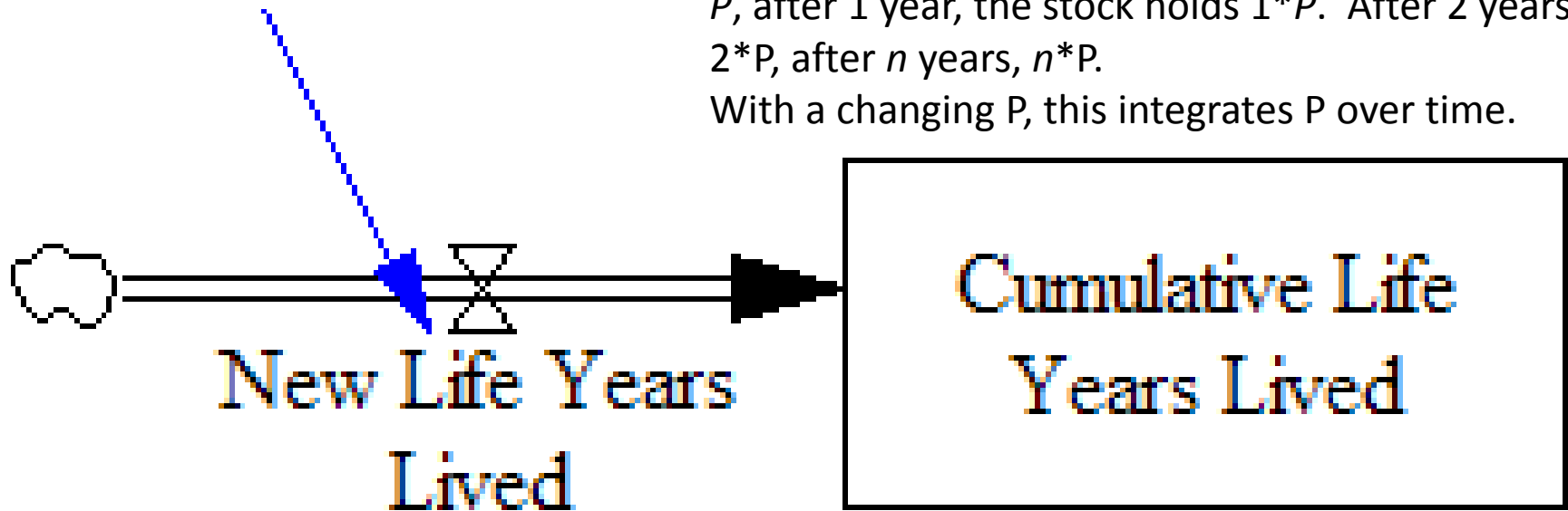


# Stocks As Accumulations

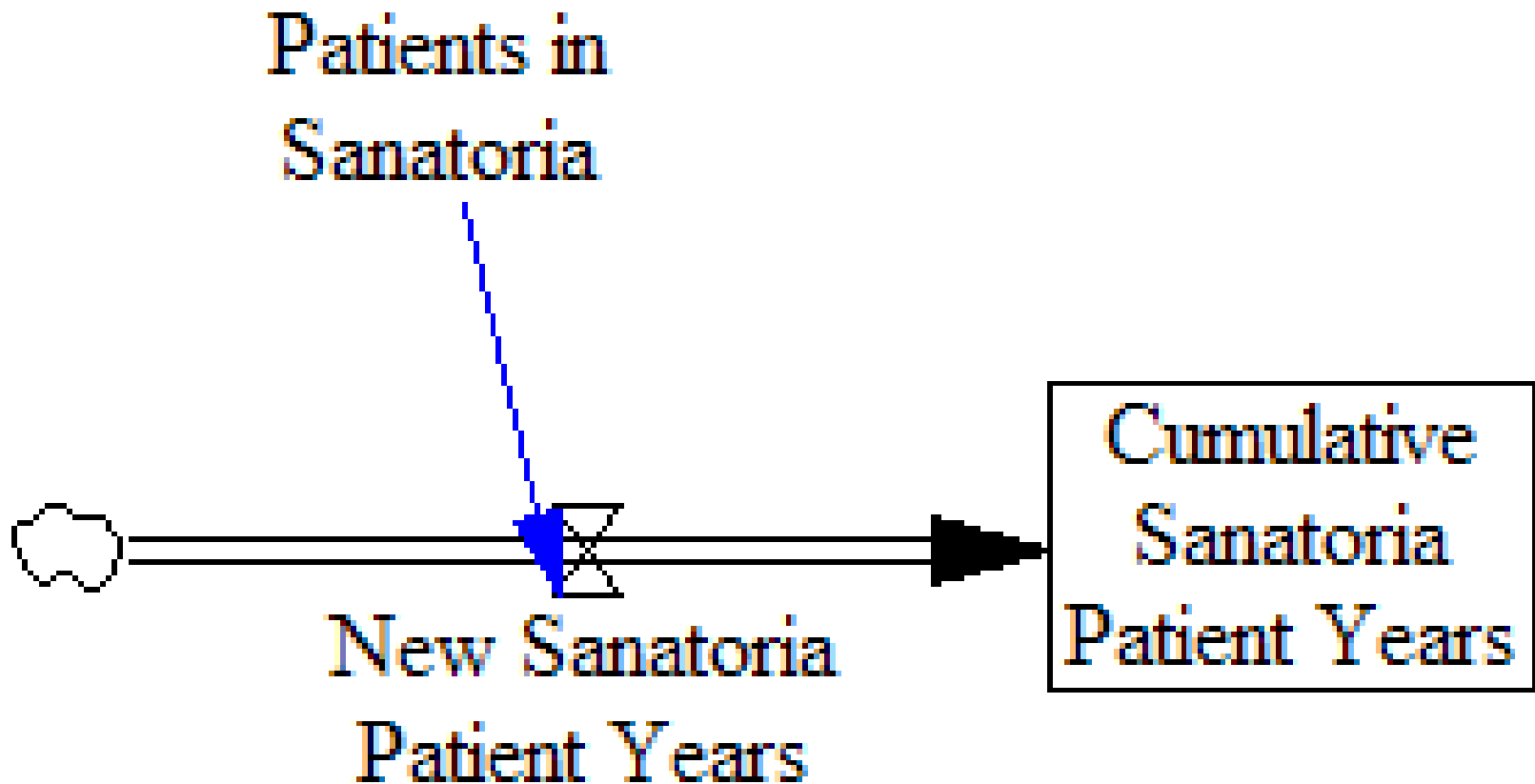
- We often use stocks to accumulate (integrate) other (evolving) quantities over time
- Example (assume time measured in years):

Current Population

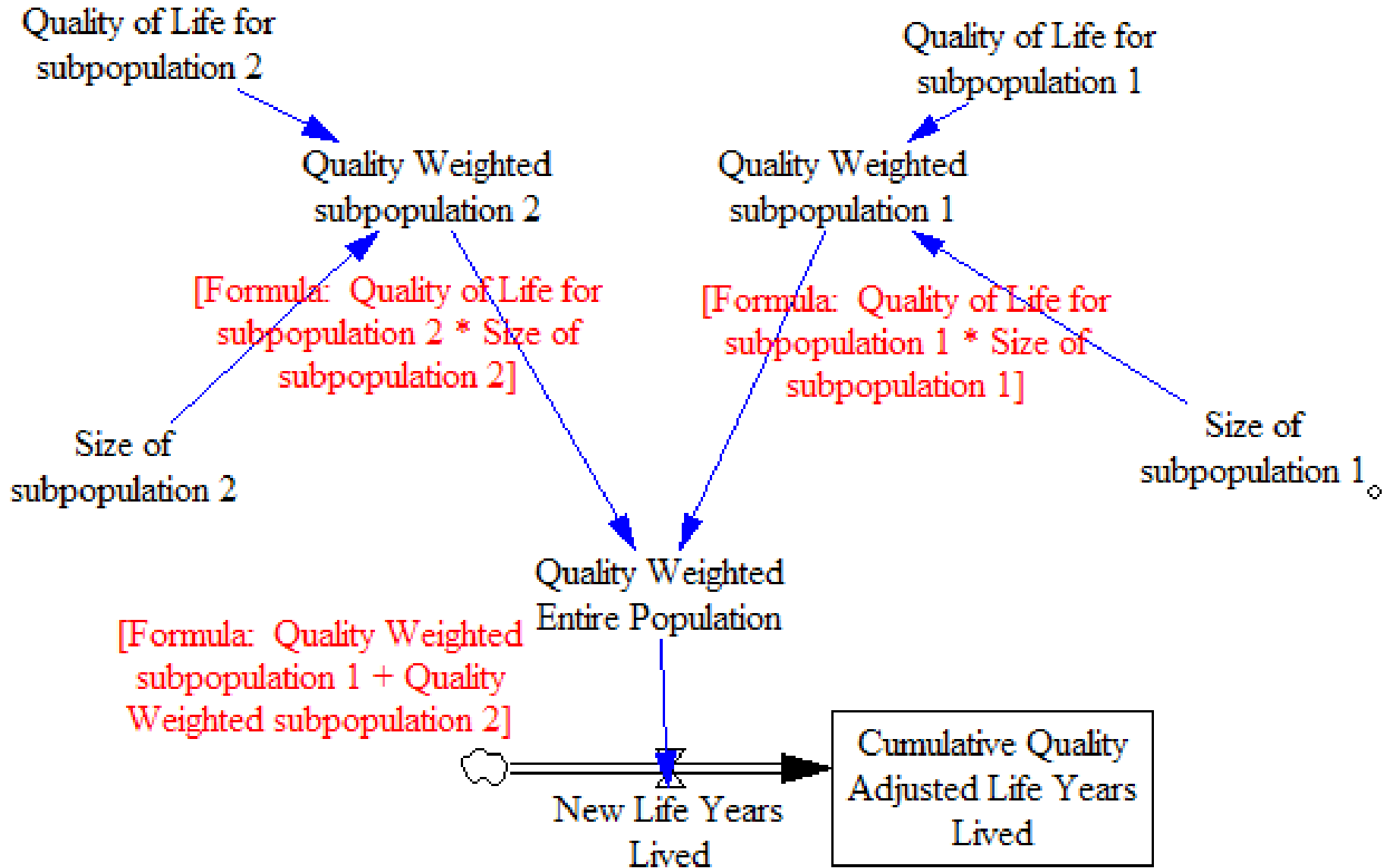
**A Key Reflection:** If we have population of size  $P$ , after 1 year, the stock holds  $1 \cdot P$ . After 2 years,  $2 \cdot P$ , after  $n$  years,  $n \cdot P$ .  
With a changing  $P$ , this integrates  $P$  over time.



# Example 2



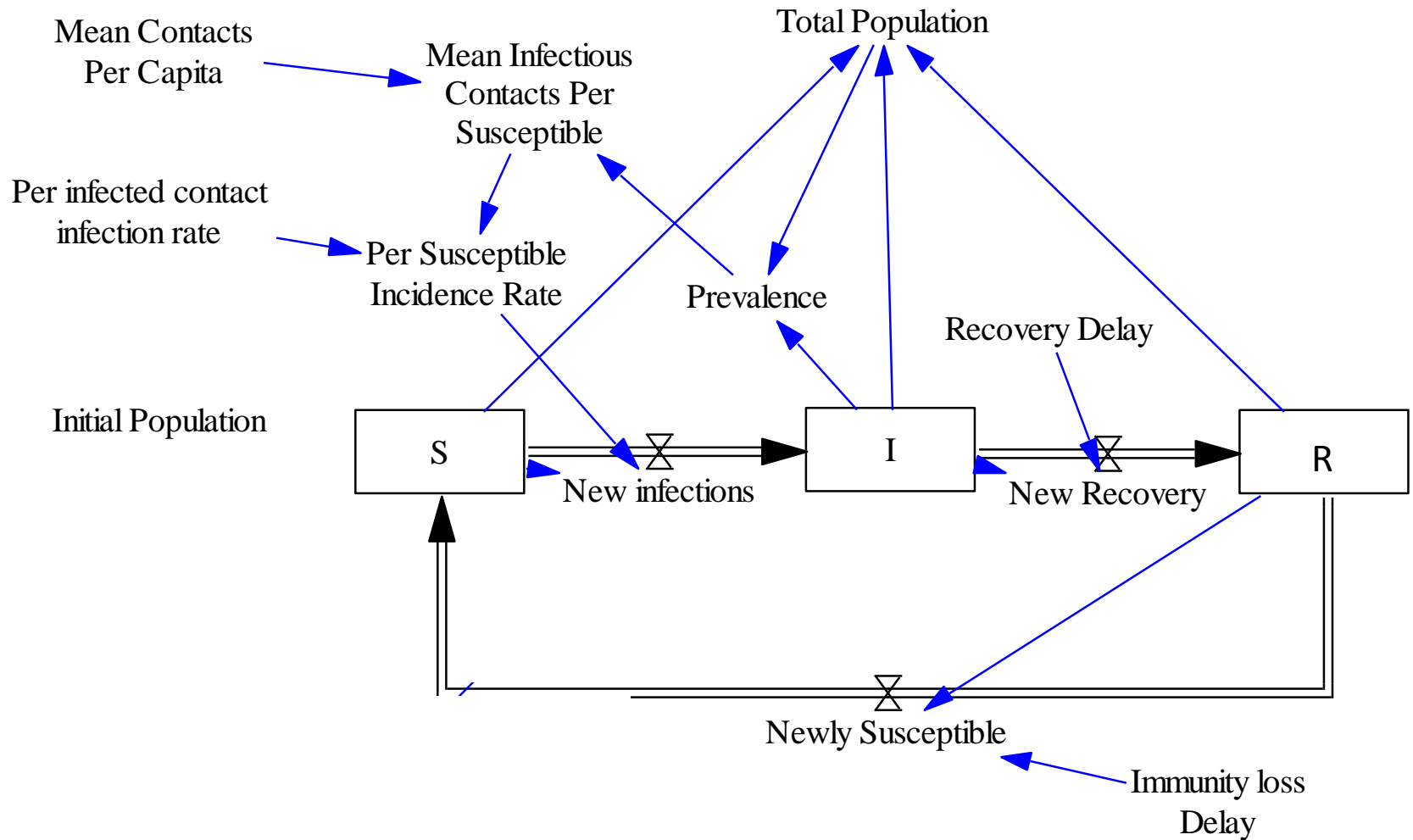
# Slightly more Sophisticated



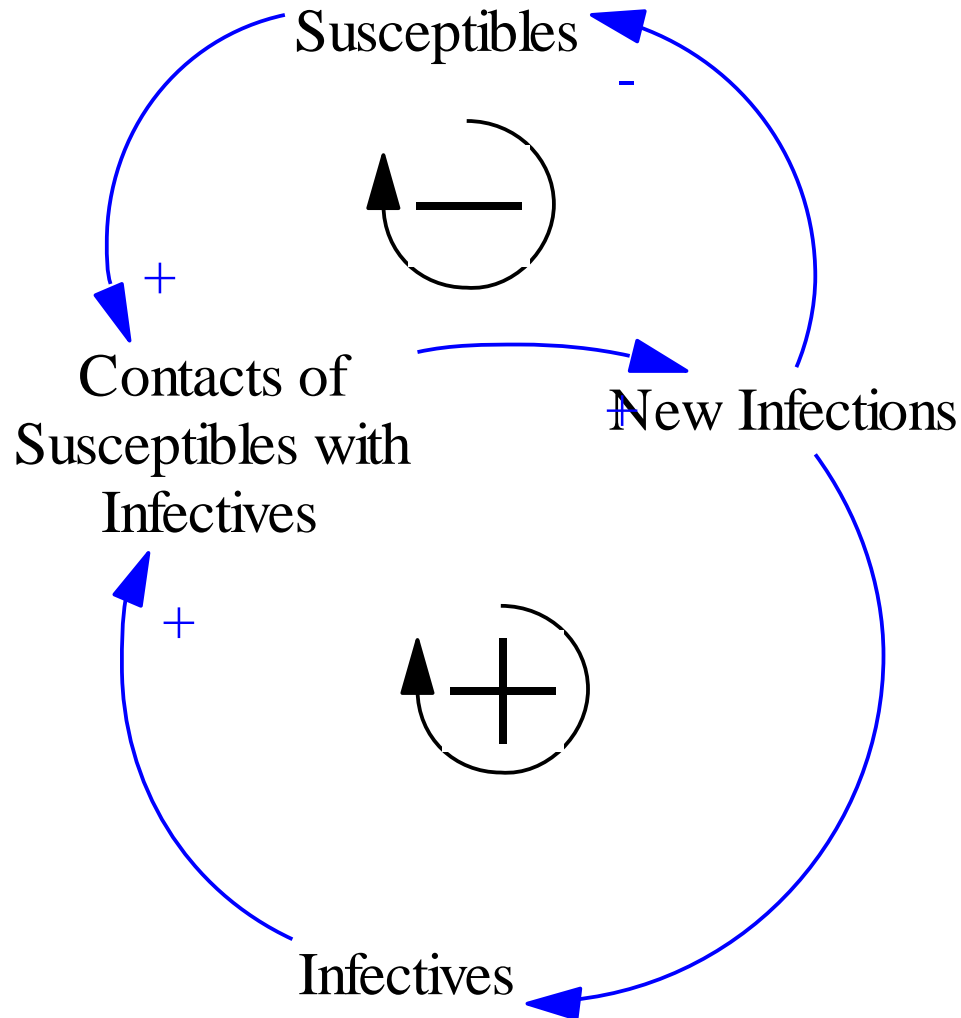
# Principle: Structure Determines Behaviour

- Feedback & stock-and-flow structure of a system determines the possible patterns of behaviour
- Different sets of parameters (e.g. values for constants) will select particular behaviour within these behaviour patterns
- Changes to the feedback structure can change behaviour in fundamental ways

# Simple SIT Model

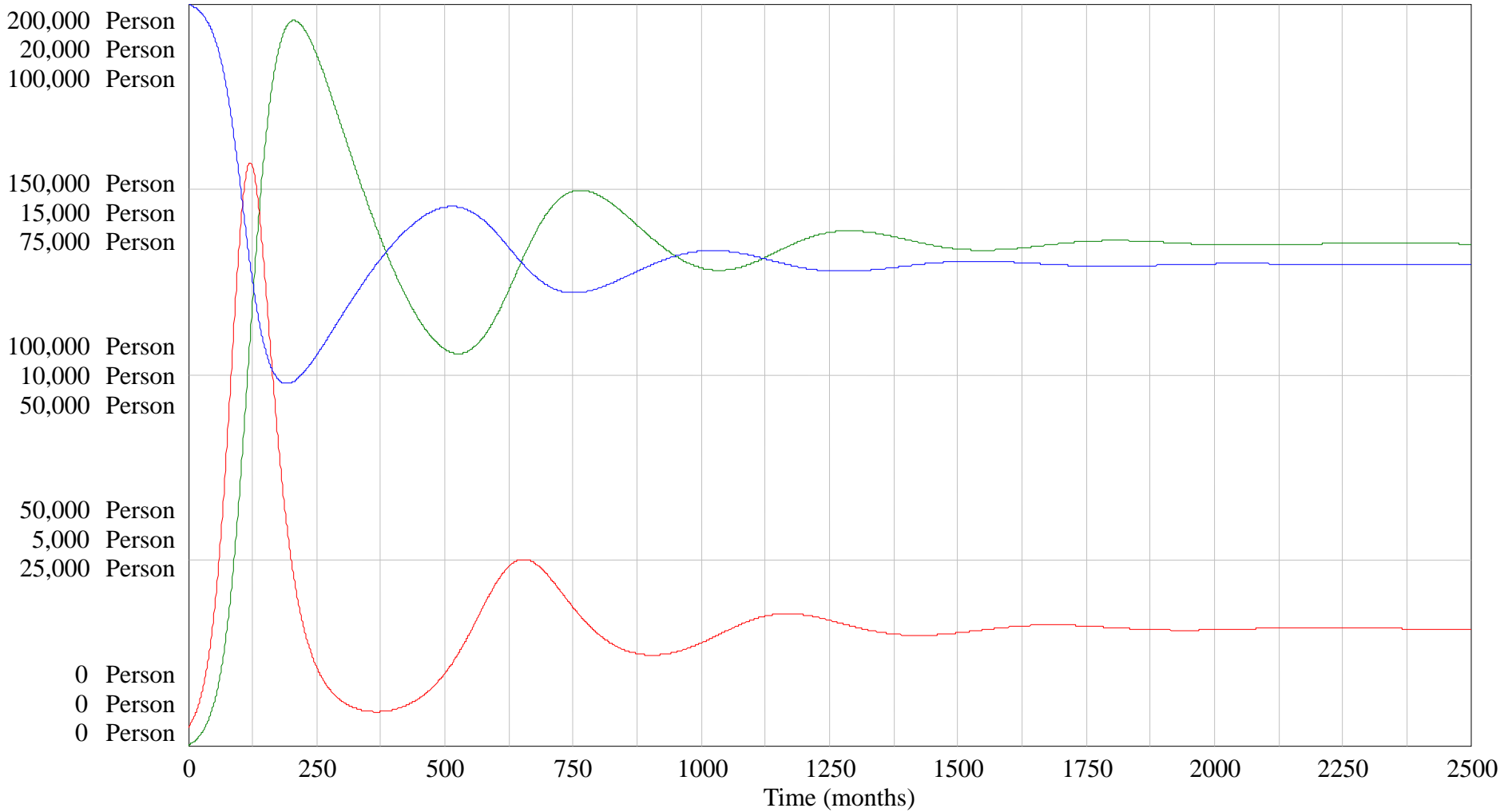


# Classic Feedbacks



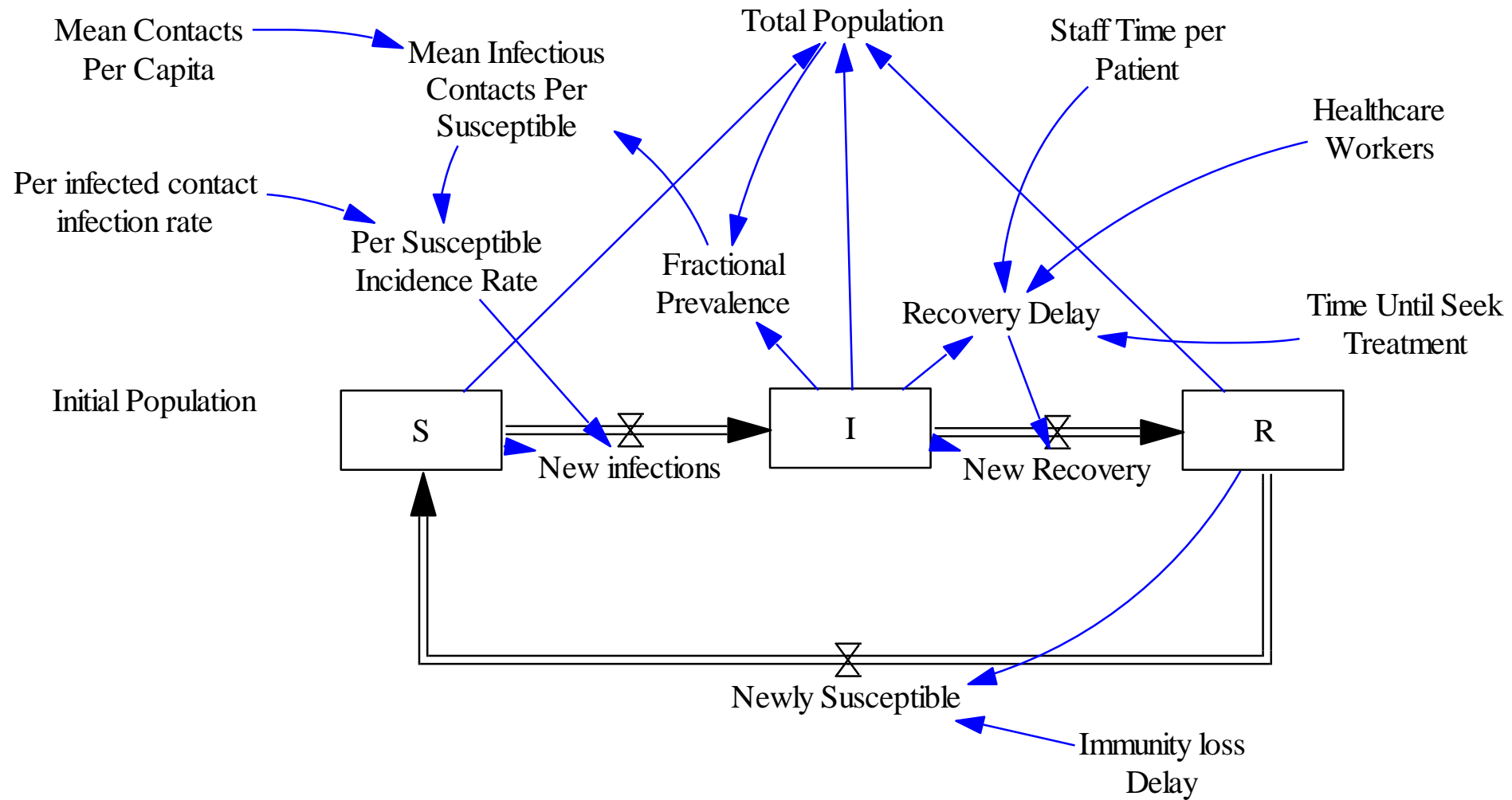
# Dynamics

State variables over time



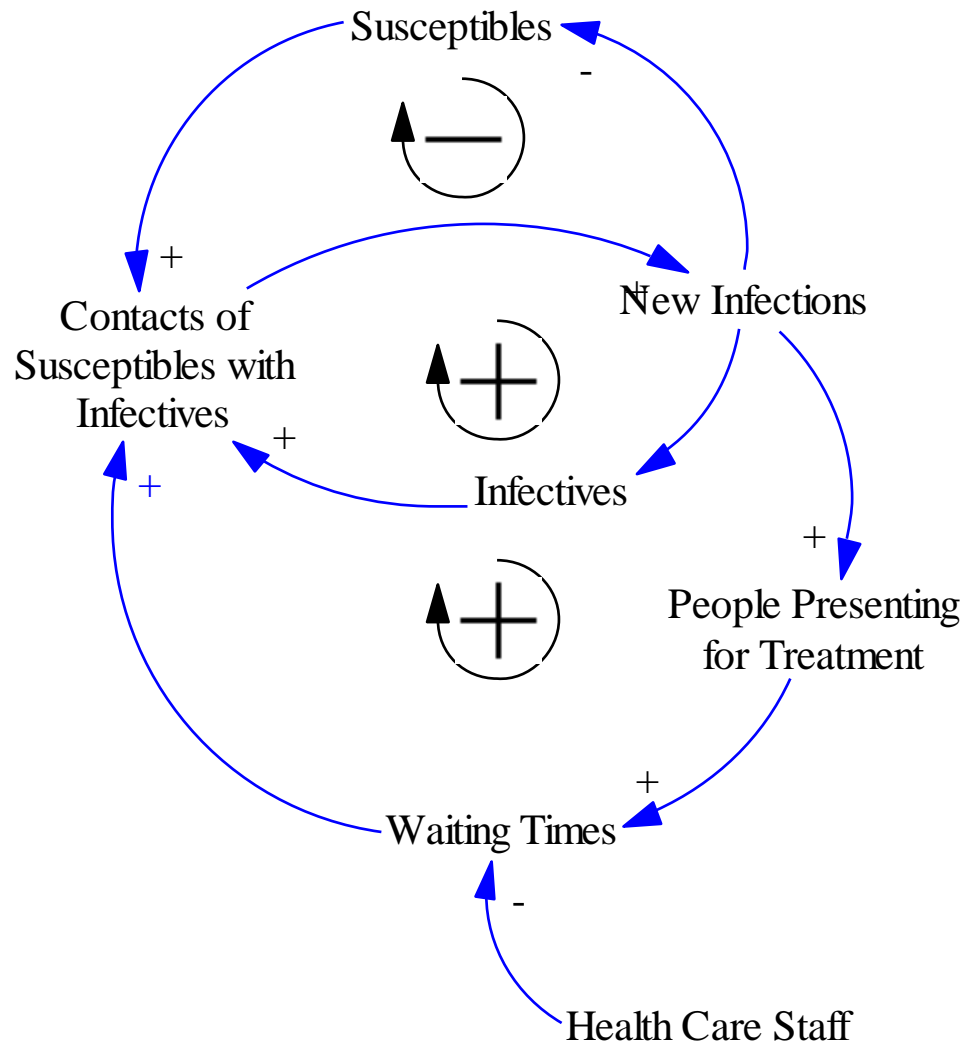
S : Alternative 30 HC Workers Exogenous Recovery Delay Person  
I : Alternative 30 HC Workers Exogenous Recovery Delay Person  
R : Alternative 30 HC Workers Exogenous Recovery Delay Person

# Broadening the Model Boundaries: Endogenous Recovery Delay



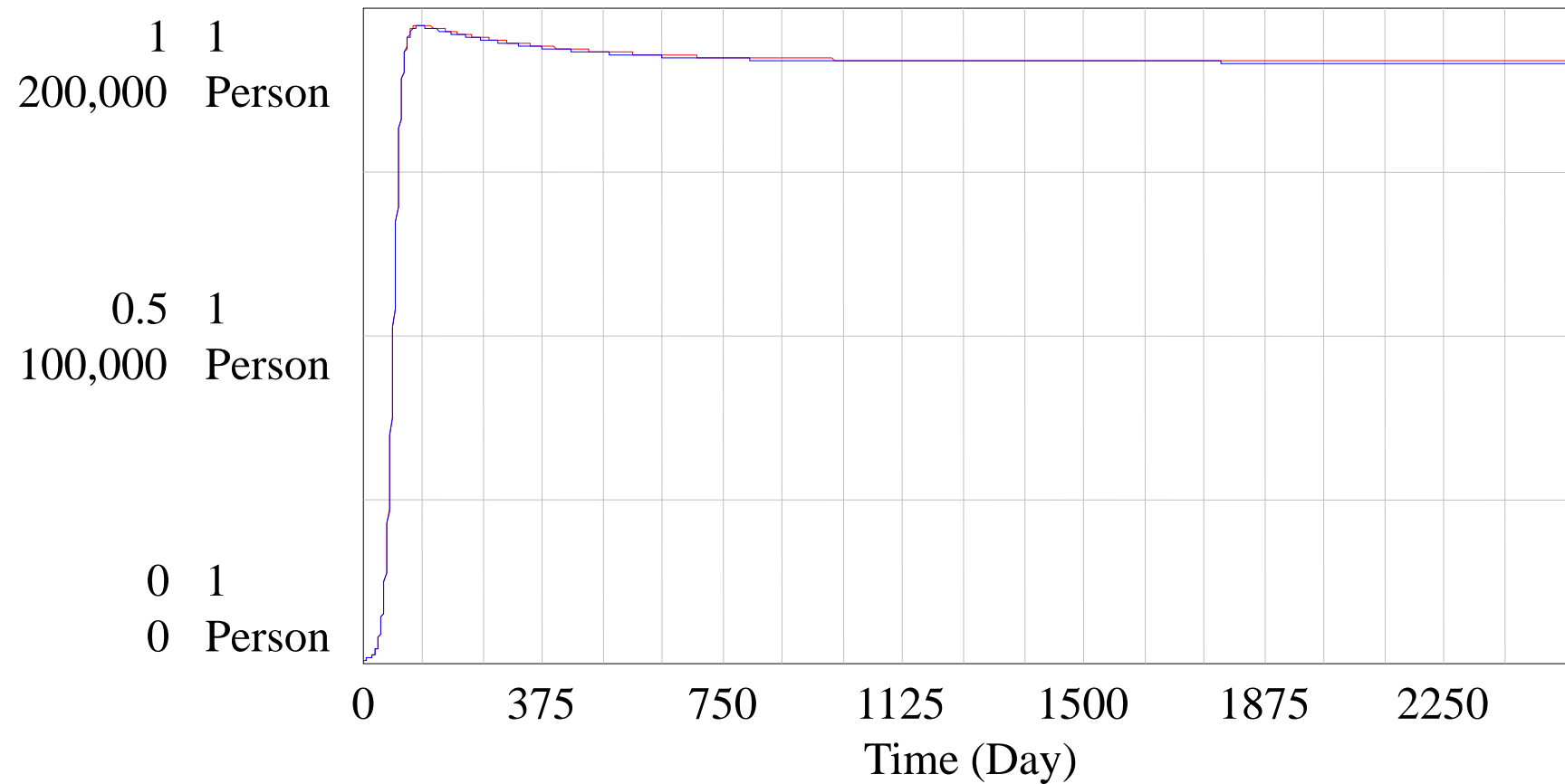


# Broadening the Model Boundaries: Endogenous Recovery Delay



# A Different Behaviour Mode

## Prevalence, Infectious



Prevalence : Baseline 30 HC Workers ————— 1  
I : Baseline 30 HC Workers ————— Person

# Structure as Shaping Behaviour

- System structure is defined by
  - Stocks
  - Flows
  - Connections between them
- Nonlinearity: The behaviour of the whole is more than the sum of the behaviour of the parts
  - “Emergent” behaviour would not be anticipated from simple behaviour of each piece in turn
- Stock and flow structure (including feedbacks) of a system determines the qualitative behaviour modes that the system can take on